

# Structural Equation Modeling for Ordinal Data

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# Outline

- 1 Two Meanings of Non-Normality
- 2 Should Ordinal Data Be Treated as Numeric Data?
  - Current common practices
  - Ordinal data should be modeled differently
  - Ordinal data can be treated as numeric (with caution!)
- 3 Estimators for categorical data
- 4 CFA Models with Ordinal Data
  - Data input/type
  - CFA Models with Ordinal Data from HBSC
- 5 Structural Models with Ordinal Data
  - Direct regressive models
  - Indirect effect (mediation) models
- 6 Measurement Invariance Testing with Ordinal Data

# Goals of this Session

During this session:

- Understand the non-normality issues in SEM
- SEM estimation
- Focus on ordinal data

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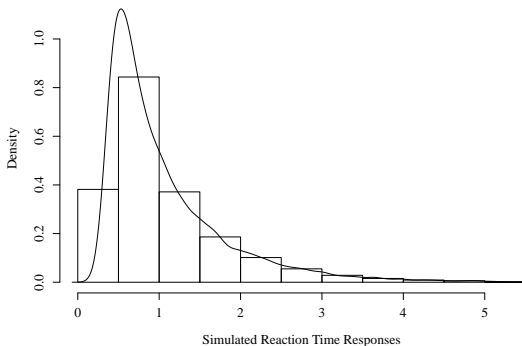
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# Meaning 1: Nonsymmetric, skewed distribution

“Non-normal data”: sample distribution is not unimodal and symmetric.

- For instance, observations are often skewed in reaction time (RT) studies.



## Meaning 1: Nonsymmetric, skewed distribution ...

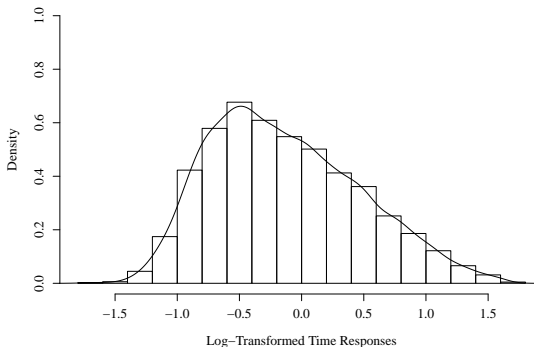
- E.g., Correll et al. (2002) conducted experimental studies on the reaction time for shooting decisions.
- Sometimes projects mathematically transform variables to make them “more normal”

### *Results and Discussion*

To analyze the resulting reaction times, we excluded all trials on which the participant had either timed-out (i.e., failed to make a decision in the allotted 850-ms window) or made an incorrect response (e.g., shooting a target holding a non-gun). This resulted in the exclusion of data from 7% of the trials across participants, with a maximum of 20% of the trials for any one participant. Response latencies on the remaining trials were log-transformed and then averaged within subject across trials occurring in the same cell of the  $2 \times 2$  within-subject research design. An analysis of variance (ANOVA) of the resulting mean latencies was then conducted, treating Target Ethnicity (White vs. African American) and Object Type (gun versus no gun) as within-subject factors.

# Meaning 1: Nonsymmetric, skewed distribution ...

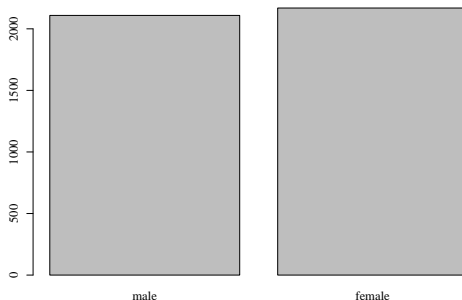
- In our example data, the log-transformed data is slightly more like a Normal distribution.





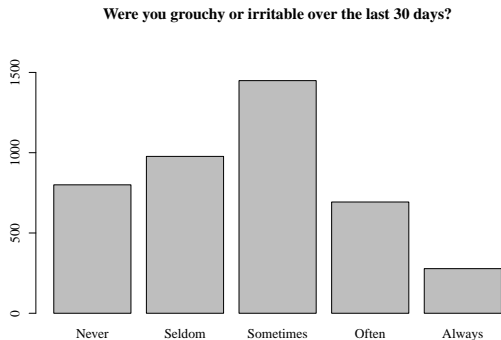
## Meaning 2: Categorical Data

- **categorical variables** are discrete groupings of observations
- nominal: unordered categories, such as gender



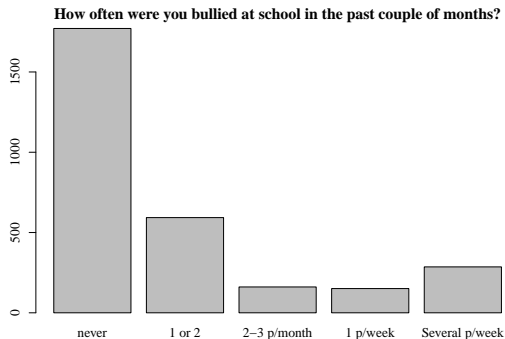
- ordinal variables: may appear unimodal, symmetric.

## Meaning 2: Categorical Data ...



- But ordinal measures are inherently non-normal by nature (discrete, non-numeric; O'Brien, 1985).

## Meaning 2: Categorical Data ...



- Models providing alternatives to the normal/numeric treatment
  - For **non-normal numeric data**, variants of the generalized linear model. These are not our primary focus today
  - For ordinal **categorical data**, new methods are more well-suited to the data. This is the focus of the remainder of this presentation.

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# Some Published Work on the Big Five Personality

|                   |          |           |       |                |
|-------------------|----------|-----------|-------|----------------|
| Strongly Disagree | Disagree | Undecided | Agree | Strongly Agree |
| 1                 | 2        | 3         | 4     | 5              |

- A variable scored  $\{1,2,3,4,5\}$  cannot be “Normal”. A normal variable is a floating point number,  $\{1,2,3,4,5\}$  are not.
- Nevertheless, it is common in many fields to treat them like numbers

## Measures.

**Big Five Inventory.** As described above, the original Big Five Inventory (BFI; John, Donahue, & Kentle, 1991; see John et al., 2008) was developed to measure the prototypical features of each Big Five domain. Its 44 items are short, descriptive phrases that respondents rate on a 5-point scale ranging from *disagree strongly* to *agree strongly*. A total of 641 ESCS members completed the BFI; in this sample, the domain scales' alpha reliabilities were .86 for Extraversion, .82 for Agreeableness, .83 for Conscientiousness, .85 for Negative Emotionality, and .84 for Open-Mindedness.

(Soto & John, 2017a)

# Treating a Likert Scale as Numbers

|                   |          |           |       |                |
|-------------------|----------|-----------|-------|----------------|
| Strongly Disagree | Disagree | Undecided | Agree | Strongly Agree |
| 1                 | 2        | 3         | 4     | 5              |

- The original SEM was designed for numeric data.
- It was standard to treat “Likert-type” variables as if they were normally distributed.

To examine the multidimensional structure of the BFI-2-S and BFI-2-XS, we submitted each short form's items to a random intercept EFA that extracted and varimax-rotated five factors, using maximum likelihood estimation. Random intercept EFA (Aichholzer, 2014) is a procedure for examining the multidimensional structure of an item set while using a method factor to model individual differences in acquiescent responding, thereby minimizing the negative structural effects of acquiescence variance (Rammstedt & Farmer, 2013; Soto et al., 2008). For both short

(Soto & John, 2017b)

# Treating a Likert Scale as Numbers ...

- In the 1980s, alternative methods became available, including “robust” standard errors and re-scaled  $\chi^2$  statistics, and wholly new estimators.

Prior to analysis, all items were checked for non-normality. Skewness and kurtosis of the data were  $-1.18$  to  $0.25$  (kurtosis) and  $-0.87$  to  $0.95$  (skewness), showing that items were mainly close to normal. Because population weights were used to draw highly precise conclusions about the population, a restricted maximum likelihood (MLR) estimator was applied (Muthén & Muthén, 1998–2013). Factor models were separately fitted for each of the Big Five traits.

Another Big Five study (Göllner et al., 2017)

- Under what conditions is it reasonable to treat an ordinal variable as if it were a numeric?

# The Long-Lasting "Interval-Ordinal Debate"

- Suppose data is a reflection of a "rounding" process, in which thresholds are imposed that separate responses into bins (as described in previous set of notes). The data may appear to be unimodal-symmetric.
- What should we do?

## There are two sides in the debate

Claim 1: Ordered-categorical data should be analyzed only using methods developed for categorical data (e.g., WLSMV).

Claim 2: Ordered-categorical data can be analyzed using methods developed for continuous data (e.g., ML or MLR), **if...**

## Support for Claim 1:

- ① Categorical model has unique theoretical features (thresholds)
- ② Less biased (more accurate) estimates
- ③ More valid statistical inferences



# The Long-Lasting "Interval-Ordinal Debate" ...

## Support for Claim 2:

Probably including

- ① The numeric software is faster, simpler (estimates fewer coefficients)
- ② Can view 1-2-3-4-5 data as "rounded" numbers.
- ③ **If** there are more than five response options, the data appear to be "normal enough"
- ④ Results are same either way, so we use the more familiar method
- ⑤ There is no suitable software for discrete data that tolerates
  - small sample size,
  - missing data

# Why (or when) ordinal data should not be treated as if it were numeric

Support 1a. - Treating ordinal data as numeric can lead to model misspecifications

*“With five-category Likert scales, the [indicator] variables are often scored by consecutive integers, say 0, 1, 2, 3, 4. The analysis then proceeds as if these [indicator] variables are interval scaled ....*

**Strictly speaking, the model cannot be correct unless there are infinitely many categories for each [indicator variable] ...”** .

*[For indicator variables based on Likert scales] with extreme skews it should further be noted that the ordinary measures of association, covariances and Pearson product moment correlations, may not be suitable. Not only the [indicator variables] discrete, but they are also limited in range with strong censoring. **In such cases, a linear model for [ordinal data] may be unrealistic, and a non-linear model ... may be more appropriate**” (B. Muthén & Kaplan, 1985, p. 172).*

# Why (or when) ordinal data should not be treated as if it were numeric ...

Support 1b. - Applying modeling techniques developed for numeric data to ordinal data can lead to incorrect parameter and global model fit estimates (Beauducel & Herzberg, 2006; Flora & Curran, 2004a).

- Spuriously inflated model  $\chi^2$  values (i.e., over-rejection of solutions)
- Modest underestimation of fit indices (e.g., TLI, CFI)
- moderate to severe underestimation of the standard errors of the parameter estimates (inflated Type I error)
- These issues are exacerbated when the sample size is small.

# Why (or when) ordinal data should not be treated as if it were numeric ...

Support 1c. - Inferences are made from valid models that align with data

Second, this study replicated previous results that factor loadings are typically underestimated by MLR but are essentially unbiased with WLSMV (Beauducel & Herzberg, 2006; DiStefano, 2002; Flora & Curran, 2004). Interestingly, a clear superiority of WLSMV over MLR in factor loading estimates was found in this study, irrespective of the number of categories. This study also revealed that the factor loadings obtained by WLSMV were more precise and accurate than those obtained by MLR when the latent normality assumption was moderately violated. Generally speaking, WLSMV was preferable to MLR across most of the conditions observed in this study, given its properties of being less biased and having small sampling variation in estimating factor loadings.

WLSMV vs. MLR (Li, 2016)



# Why (or when) ordinal data should not be treated as if it were numeric ... ..

Support 1d. - Treating categorical as continuous is fundamentally wrong

*“The usual numerical values assigned to these dichotomous variables are the ad hoc numbers '1' and '0', or '1' and '2'. Hence, the basic assumption that the data come from a continuous normal distribution **is clearly violated**. In fact, even for polytomous variables that are closer to continuous variables than dichotomous variables, ignoring the discrete nature of the data **leads to erroneous results**”.*

BSEM with dichotomous variables (Lee & Song, 2003, p. 3074)

*“In behavioral and social sciences research, many variables are only observed in dichotomous or polytomous form. Examples of such variables are attitude items, performance items, rating scales, etc. When analyzing this kind of data, **a common approach used by nonrigorous statisticians** is to assign integral values to the categories and proceed as if the data are measured on an interval scale”.*

# Why (or when) ordinal data should not be treated as if it were numeric ... ..

BSEM with polytomous variables (Song & Lee, 2002, p. 453)

# Why (or when) ordinal data can be treated as if is numeric

If there are more categories (Bollen & Barb, 1981, p. 234) correlations are less incorrect

# Why (or when) ordinal data can be treated as if is numeric

## AMERICAN SOCIOLOGICAL REVIEW

Table 1. Comparison of Mean Correlation Coefficients for Original and Collapsed Variables

| Number of<br>Categories                  | Mean Collapsed Correlation |              |              |              |              |
|--|----------------------------|--------------|--------------|--------------|--------------|
|  | 2                          | 0.117        | 0.264        | 0.414        | 0.579        |
| 3  | 0.149                      | 0.302        | 0.445        | 0.617        | 0.727        |
| 4  | 0.165                      | 0.336        | 0.504        | 0.669        | 0.774        |
| 5  | 0.182                      | 0.359        | 0.533        | 0.712        | 0.806        |
| 6  | 0.180                      | 0.371        | 0.554        | 0.733        | 0.833        |
| 7  | 0.192                      | 0.380        | 0.563        | 0.750        | 0.850        |
| 8  | 0.193                      | 0.384        | 0.571        | 0.760        | 0.860        |
| 9  | 0.194                      | 0.389        | 0.577        | 0.771        | 0.870        |
| 10                                       | 0.197                      | 0.391        | 0.581        | 0.772        | 0.875        |
| <b>Mean<br/>Original<br/>Correlation</b> | <b>0.203</b>               | <b>0.404</b> | <b>0.599</b> | <b>0.796</b> | <b>0.901</b> |

Based on 50 samples of 500 observations each.



# Why (or when) ordinal data can be treated as if is numeric

...

WLSM and WLSMV also reported sensitivity to extreme levels of nonnormality, but generally, with more categories (five, seven) and smaller sample sizes (200, 400). Under these conditions, WLSMV reported greater numbers of replications that did not converge than with the two- or three-category conditions. With many categories and item-level nonnormality, a contingency table between two observed variables could result in empty cells. The *Mplus* Web site noted the sensitivity of categorical estimators to empty cells and the software has implemented procedures to assist with categorical estimation beginning with *Mplus* version 4.0 (<http://www.statmodel.com>); however, some sensitivity to these conditions remains.

DiStefano and Morgan (2014, p. 430); also see Flora and Curran (2004a)

## More serious issue: missing data treatment

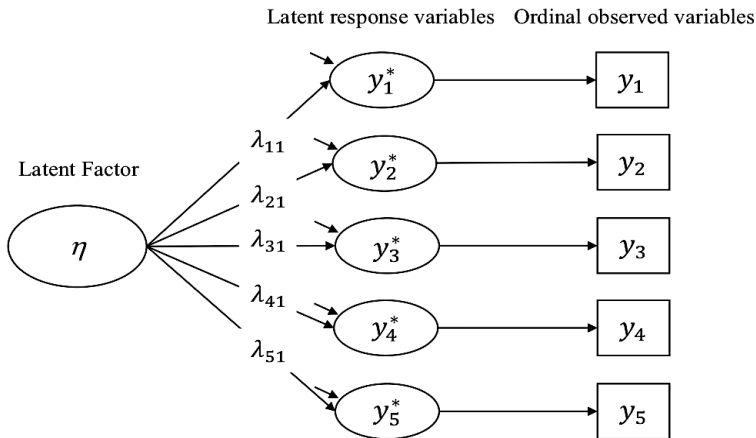
- Categorical estimators (e.g., DWLS, WLSMV) require pairwise complete covariance matrix, which causes some distortion.
- Full information maximum likelihood (FIML; Arbuckle,1996) not universally available or practical for categorical variables.

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# Conceptual Framework: Thresholds

- There is an “intermediate” latent variable  $y_1^*$  which is revealed to us as a categorical outcome  $y_1$ .

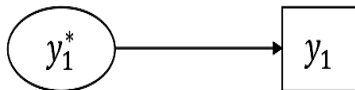


# Conceptual Framework: Thresholds ...

Flora and Curran (2004b, p. 473)

- 2 Assume  $(y_j^*)$  is a normally distributed gives rise to an ordinal observation  $y_j$  that can fall into a discrete category ( $c$ ; e.g.,  $c = 1 =$  “strongly disagree”)

Latent response variables      Ordinal observed variables

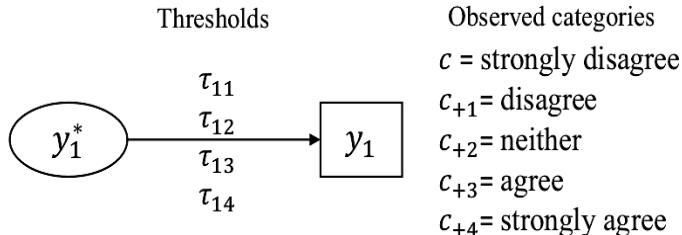


- 3 Assume there are threshold parameters ( $\tau_j$ ; tau). As  $y_j^*$  rises, it surpasses thresholds that separate the categories (e.g., from “strongly disagree” to “disagree”)

$$y_j = c, \text{ if } \tau_c < y_j^* < \tau_{c+1}$$

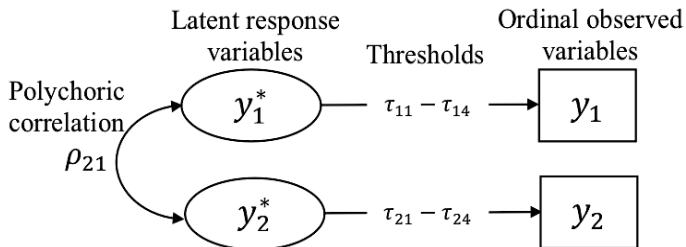
# Conceptual Framework: Thresholds

|                   |          |           |       |                |
|-------------------|----------|-----------|-------|----------------|
| Strongly Disagree | Disagree | Undecided | Agree | Strongly Agree |
| 1                 | 2        | 3         | 4     | 5              |



- A polychoric correlation ( $\rho$ ) attempts to measure the correlation between 2 normally distributed variables that “underlie” 2 categorical variables.

## Conceptual Framework: Thresholds ...



# Polychoric correlations

- SEM software is designed to align covariance (or correlation) matrices
- The earliest strategies for categorical data used a polychoric correlation based on a threshold model to compare observed and theoretical covariance.
- polychoric correlations will replace the usual Pearson product-moment correlation matrix in the usual ML estimation for SEM

$$\Sigma(\theta) = \Lambda\Psi\Lambda' + \Theta_{\epsilon}$$

This substitution approach will generally yield consistent parameter estimates.

- Robust standard errors and mean/variance adjusted Chi-square statistics will be needed (Hence, the model is sometimes referred to as “WLSMV”, rather than just “WLS”).



# WLS estimators for categorical data

- 1 WLS - fully weighted least squares fitting function

$$F_{WLS} = [s - \sigma(\theta)]'W^{-1}[s - \sigma(\theta)]$$

- 1  $s$  is a vector of sample statistics (i.e., polychoric correlations and threshold estimates)
  - 2  $\sigma(\theta)$  is the model-implied vector of population elements in  $\Sigma(\theta)$
  - 3  $W$  is weight matrix.
- 2 Diagonally weighted least squares (developed to facilitate model estimation)
    - 1 DWLS - diagonal weighted least squares

$$F_{DWLS} = [s - \sigma(\theta)]'V^{-1}[s - \sigma(\theta)]$$

- 2  $V$  is a diagonal matrix (has 0's on all elements except main diagonal)
  - 3 Once parameter estimates are obtained using the DWLS fitting function, full  $W$  matrix used to calculate standard errors
- 3 WLSMV - weighted least squares-mean adjusted

# WLS estimators for categorical data ...

- 1 In addition to using a diagonal weight matrix ( $V$ ) and standard error corrections, Muthen(1993) developed a robust goodness-of-fit test via calculation of a mean- and variance-adjusted chi-square test statistics.
- 2 Calculation of WLSMV goodness-of-fit also involves the full  $W$  matrix, however it does not involve inversion.

# Summary

- 1 Threshold estimates link observed ordinal responses to latent response variables
- 2 Polychoric correlations and full weighted least squares incorporate latent response variables into traditional SEM (common factor) framework
- 3 DWLS facilitates model estimations and provides corrected parameter standard errors
- 4 WLSMV provides more accurate goodness-of-fit statistics

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# The HBSC data

The demonstration data - a subset of HBSC Health Behaviour in School-Aged Children

```
str(hbsc)
```

```
'data.frame': 4284 obs. of 89 variables:
 $ stud_id : int 1 3 4 5 7 10 15 16 17 20 ...
 $ schl_id : int 101 66 170 169 58 109 180 66 61 24 ...
 $ Gender : Factor w/ 2 levels "male","female": 1 1 1 2 2 1 2 2 1 1 ...
 $ Age : int 13 13 12 12 13 11 12 12 11 12 ...
 $ Grade : int 7 7 6 6 7 6 6 7 6 6 ...
 $ body1_o : Ord.factor w/ 5 levels "SA"<"A"<"U"<"D"<...: 4 4 NA NA 4 3
 5 4 NA NA ...
 $ body2_o : Ord.factor w/ 5 levels "SA"<"A"<"U"<"D"<...: 4 4 NA NA 4 2
 1 4 NA NA ...
 $ body3_o : Ord.factor w/ 5 levels "SA"<"A"<"U"<"D"<...: 5 5 NA NA 4 3
 5 3 NA NA ...
 $ body4_o : Ord.factor w/ 5 levels "SA"<"A"<"U"<"D"<...: 5 4 NA NA 4 3
 4 3 NA NA ...
 $ body5_o : Ord.factor w/ 5 levels "SA"<"A"<"U"<"D"<...: 5 5 NA NA 5 3
 5 3 NA NA ...
 $ phys1_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 4 1 5 5
 5 5 4 5 5 3 ...
```

# The HBSC data ...

```

$ phys2_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 4 5 5
  5 2 4 5 5 4 ...
$ phys3_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 2 5 1
  5 2 2 3 5 5 ...
$ phys4_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 5 5 5
  5 1 5 5 5 5 ...
$ phys5_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 4 5 4
  4 1 4 5 5 4 ...
$ phys6_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 2 5 4
  4 1 3 4 5 5 ...
$ phys7_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 1 5 5
  3 1 3 1 5 5 ...
$ phys8_o : Ord.factor w/ 5 levels "EveryDay"<"EveryWeek"<...: 5 5 5 5
  5 1 4 5 5 4 ...
$ depre1_o : Ord.factor w/ 5 levels "Never"<"Seldom"<...: 2 2 3 3 2 3 1
  3 1 1 ...
$ depre2_o : Ord.factor w/ 5 levels "Never"<"Seldom"<...: 2 2 4 5 3 4 4
  3 1 2 ...
$ depre3_o : Ord.factor w/ 5 levels "Never"<"Seldom"<...: 1 5 2 3 2 4 1
  1 1 1 ...
$ depre4_o : Ord.factor w/ 5 levels "Never"<"Seldom"<...: 1 2 1 5 1 1 3
  1 3 2 ...
$ depre5_o : Ord.factor w/ 5 levels "Never"<"Seldom"<...: 2 2 1 3 3 1 3
  1 1 1 ...
$ depre6_o : Ord.factor w/ 5 levels "Never"<"Seldom"<...: 1 2 1 5 1 5 1
  1 1 2 ...

```

# The HBSC data ...

```

$ gotBu1_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 2 1 1 1 NA
  NA 1 1 1 ...
$ gotBu2_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ gotBu3_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ gotBu4_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 3 1 NA
  NA 1 1 2 ...
$ gotBu5_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 2 1 1 1 NA
  NA 1 1 1 ...
$ gotBu6_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 4 1 NA
  NA 1 1 1 ...
$ gotBu7_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ gotBu8_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 NA 1 NA
  NA 1 1 2 ...
$ gotBu9_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 5 1 NA
  NA 1 1 1 ...
$ bu0th1_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 2 1 1 4 1 NA
  NA 1 1 1 ...
$ bu0th2_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ bu0th3_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 4 1 NA
  NA 1 1 2 ...
$ bu0th4_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...

```

# The HBSC data ...

```

$ bu0th5_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ bu0th6_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ bu0th7_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ bu0th8_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ bu0th9_o: Ord.factor w/ 5 levels "never"<"1 or 2"<...: 1 1 1 1 1 NA
  NA 1 1 1 ...
$ alc1_o  : Ord.factor w/ 5 levels "Never"<"Rarely"<...: 1 1 1 1 1 2 1
  2 1 1 ...
$ alc2_o  : Ord.factor w/ 5 levels "Never"<"Rarely"<...: 1 1 1 1 1 1 1
  1 1 1 ...
$ alc3_o  : Ord.factor w/ 5 levels "Never"<"Rarely"<...: 1 1 1 1 1 1 1
  1 1 1 ...
$ alc4_o  : Ord.factor w/ 5 levels "Never"<"Rarely"<...: 1 1 1 1 1 1 1
  2 1 1 ...
$ alc5_o  : Ord.factor w/ 5 levels "Never"<"Rarely"<...: 1 1 1 1 1 1 1
  1 1 1 ...
$ body1_i : int    4 4 NA NA 4 3 5 4 NA NA ...
$ body2_i : int    4 4 NA NA 4 2 1 4 NA NA ...
$ body3_i : int    5 5 NA NA 4 3 5 3 NA NA ...
$ body4_i : int    5 4 NA NA 4 3 4 3 NA NA ...
$ body5_i : int    5 5 NA NA 5 3 5 3 NA NA ...
$ phys1_i : int    4 1 5 5 5 5 4 5 5 3 ...

```



# The HBSC data ...

```

55  $$ phys2_i : int    5 4 5 5 5 2 4 5 5 4 ...
    $$ phys3_i : int    5 2 5 1 5 2 2 3 5 5 ...
    $$ phys4_i : int    5 5 5 5 5 1 5 5 5 5 ...
    $$ phys5_i : int    5 4 5 4 4 1 4 5 5 4 ...
    $$ phys6_i : int    5 2 5 4 4 1 3 4 5 5 ...
50  $$ phys7_i : int    5 1 5 5 3 1 3 1 5 5 ...
    $$ phys8_i : int    5 5 5 5 5 1 4 5 5 4 ...
    $$ depre1_i : int   2 2 3 3 2 3 1 3 1 1 ...
    $$ depre2_i : int   2 2 4 5 3 4 4 3 1 2 ...
    $$ depre3_i : int   1 5 2 3 2 4 1 1 1 1 ...
55  $$ depre4_i : int   1 2 1 5 1 1 3 1 3 2 ...
    $$ depre5_i : int   2 2 1 3 3 1 3 1 1 1 ...
    $$ depre6_i : int   1 2 1 5 1 5 1 1 1 2 ...
    $$ gotBu1_i : int   1 2 1 1 1 NA NA 1 1 1 ...
    $$ gotBu2_i : int   1 1 1 1 1 NA NA 1 1 1 ...
70  $$ gotBu3_i : int   1 1 1 1 1 NA NA 1 1 1 ...
    $$ gotBu4_i : int   1 1 1 3 1 NA NA 1 1 2 ...
    $$ gotBu5_i : int   1 2 1 1 1 NA NA 1 1 1 ...
    $$ gotBu6_i : int   1 1 1 4 1 NA NA 1 1 1 ...
    $$ gotBu7_i : int   1 1 1 1 1 NA NA 1 1 1 ...
75  $$ gotBu8_i : int   1 1 1 NA 1 NA NA 1 1 2 ...
    $$ gotBu9_i : int   1 1 1 5 1 NA NA 1 1 1 ...
    $$ bu0th1_i : int   2 1 1 4 1 NA NA 1 1 1 ...
    $$ bu0th2_i : int   1 1 1 1 1 NA NA 1 1 1 ...
    $$ bu0th3_i : int   1 1 1 4 1 NA NA 1 1 2 ...
80  $$ bu0th4_i : int   1 1 1 1 1 NA NA 1 1 1 ...

```

# The HBSC data ...

```
35  $$ bu0th5_i: int 1 1 1 1 1 NA NA 1 1 1 ...
    $$ bu0th6_i: int 1 1 1 1 1 NA NA 1 1 1 ...
    $$ bu0th7_i: int 1 1 1 1 1 NA NA 1 1 1 ...
    $$ bu0th8_i: int 1 1 1 1 1 NA NA 1 1 1 ...
    $$ bu0th9_i: int 1 1 1 1 1 NA NA 1 1 1 ...
    $$ alc1_i : int 1 1 1 1 1 2 1 2 1 1 ...
    $$ alc2_i : int 1 1 1 1 1 1 1 1 1 1 ...
    $$ alc3_i : int 1 1 1 1 1 1 1 1 1 1 ...
    $$ alc4_i : int 1 1 1 1 1 1 1 2 1 1 ...
    00  $$ alc5_i : int 1 1 1 1 1 1 1 1 1 1 ...
```

# The nature of your data

- Check that the levels are meaningfully ordered

```
## An ordered-factor variable in R should look like
levels(hbsc$depre1_o)
```

```
[1] "Never"      "Seldom"     "Sometimes"  "Often"      "Always"
```

```
str(hbsc$depre1_o)
```

```
Ord.factor w/ 5 levels "Never"<"Seldom"<...: 2 2 3 3 2 3 1 3 1 1 ...
```

# A one-factor categorical CFA model

```
## Specifying the model-structure object
cfa.01.ord <- '
  depress =~ NA*depre1_o + depre2_o + depre3_o +
              depre4_o + depre5_o + depre6_o
  depress ~ 1*depress '
## Estimating the model
cfa.01.ord.fit <-
  cfa(model = cfa.01.ord, data = hbsc,
      mimic = "Mplus", estimator = "WLSMV",
      ordered = c("depre1_o", "depre2_o",
                  "depre3_o", "depre4_o",
                  "depre5_o", "depre6_o"))
## Requesting an estimation summary
summary(cfa.01.ord.fit, fit.measures = TRUE,
        standardized = TRUE)
```

# A one-factor categorical CFA model ...

```

lavaan 0.6-3 ended normally after 12 iterations

Optimization method                NLMINB
Number of free parameters           30

Number of observations              Used      Total
                                   4103     4284

Estimator                          DWLS      Robust
Model Fit Test Statistic            170.031   315.344
Degrees of freedom                   9         9
P-value (Chi-square)                0.000     0.000
Scaling correction factor            0.540
Shift parameter                      0.231
  for simple second-order correction (WLSMV)

Model test baseline model:

Minimum Function Test Statistic     16019.445  10984.581
Degrees of freedom                   15         15
P-value                              0.000     0.000

User model versus baseline model:

Comparative Fit Index (CFI)         0.990     0.972

```

# A one-factor categorical CFA model ...

```

Tucker-Lewis Index (TLI)                0.983        0.953
Robust Comparative Fit Index (CFI)                NA
Robust Tucker-Lewis Index (TLI)                NA
30
Root Mean Square Error of Approximation:
RMSEA                0.066        0.091
90 Percent Confidence Interval    0.058    0.075    0.083
    0.100
P-value RMSEA <= 0.05                0.001        0.000
35
Robust RMSEA                NA
90 Percent Confidence Interval    NA
    NA
40
Standardized Root Mean Square Residual:
SRMR                0.034        0.034
45
Weighted Root Mean Square Residual:
WRMR                2.088        2.088

Parameter Estimates:

```

# A one-factor categorical CFA model ...

| Information                      |          |         | Expected     |         |        |         |
|----------------------------------|----------|---------|--------------|---------|--------|---------|
| Information saturated (h1) model |          |         | Unstructured |         |        |         |
| Standard Errors                  |          |         | Robust.sem   |         |        |         |
| <b>Latent Variables:</b>         |          |         |              |         |        |         |
|                                  | Estimate | Std.Err | z-value      | P(> z ) | Std.lv | Std.all |
| depress =~                       |          |         |              |         |        |         |
| depre1_o                         | 0.710    | 0.010   | 69.611       | 0.000   | 0.710  | 0.710   |
| depre2_o                         | 0.655    | 0.011   | 59.557       | 0.000   | 0.655  | 0.655   |
| depre3_o                         | 0.744    | 0.011   | 66.206       | 0.000   | 0.744  | 0.744   |
| depre4_o                         | 0.715    | 0.011   | 66.123       | 0.000   | 0.715  | 0.715   |
| depre5_o                         | 0.603    | 0.013   | 47.851       | 0.000   | 0.603  | 0.603   |
| depre6_o                         | 0.589    | 0.013   | 45.786       | 0.000   | 0.589  | 0.589   |
| <b>Intercepts:</b>               |          |         |              |         |        |         |
|                                  | Estimate | Std.Err | z-value      | P(> z ) | Std.lv | Std.all |
| .depre1_o                        | 0.000    |         |              |         | 0.000  | 0.000   |
| .depre2_o                        | 0.000    |         |              |         | 0.000  | 0.000   |
| .depre3_o                        | 0.000    |         |              |         | 0.000  | 0.000   |
| .depre4_o                        | 0.000    |         |              |         | 0.000  | 0.000   |
| .depre5_o                        | 0.000    |         |              |         | 0.000  | 0.000   |
| .depre6_o                        | 0.000    |         |              |         | 0.000  | 0.000   |
| depress                          | 0.000    |         |              |         | 0.000  | 0.000   |
| <b>Thresholds:</b>               |          |         |              |         |        |         |
|                                  | Estimate | Std.Err | z-value      | P(> z ) | Std.lv | Std.all |

# A one-factor categorical CFA model ...

|             |        |       |         |       |        |        |
|-------------|--------|-------|---------|-------|--------|--------|
| depre1_o t1 | -0.564 | 0.021 | -27.187 | 0.000 | -0.564 | -0.564 |
| depre1_o t2 | 0.133  | 0.020 | 6.756   | 0.000 | 0.133  | 0.133  |
| depre1_o t3 | 1.095  | 0.024 | 44.708  | 0.000 | 1.095  | 1.095  |
| depre1_o t4 | 1.786  | 0.036 | 49.021  | 0.000 | 1.786  | 1.786  |
| depre2_o t1 | -0.870 | 0.023 | -38.650 | 0.000 | -0.870 | -0.870 |
| depre2_o t2 | -0.193 | 0.020 | -9.812  | 0.000 | -0.193 | -0.193 |
| depre2_o t3 | 0.737  | 0.022 | 34.072  | 0.000 | 0.737  | 0.737  |
| depre2_o t4 | 1.510  | 0.030 | 49.857  | 0.000 | 1.510  | 1.510  |
| depre3_o t1 | 0.289  | 0.020 | 14.542  | 0.000 | 0.289  | 0.289  |
| depre3_o t2 | 0.668  | 0.021 | 31.451  | 0.000 | 0.668  | 0.668  |
| depre3_o t3 | 1.177  | 0.025 | 46.350  | 0.000 | 1.177  | 1.177  |
| depre3_o t4 | 1.624  | 0.033 | 49.899  | 0.000 | 1.624  | 1.624  |
| depre4_o t1 | -0.107 | 0.020 | -5.446  | 0.000 | -0.107 | -0.107 |
| depre4_o t2 | 0.255  | 0.020 | 12.894  | 0.000 | 0.255  | 0.255  |
| depre4_o t3 | 0.888  | 0.023 | 39.214  | 0.000 | 0.888  | 0.888  |
| depre4_o t4 | 1.436  | 0.029 | 49.520  | 0.000 | 1.436  | 1.436  |
| depre5_o t1 | -0.370 | 0.020 | -18.421 | 0.000 | -0.370 | -0.370 |
| depre5_o t2 | 0.072  | 0.020 | 3.668   | 0.000 | 0.072  | 0.072  |
| depre5_o t3 | 0.669  | 0.021 | 31.481  | 0.000 | 0.669  | 0.669  |
| depre5_o t4 | 1.232  | 0.026 | 47.292  | 0.000 | 1.232  | 1.232  |
| depre6_o t1 | -0.428 | 0.020 | -21.173 | 0.000 | -0.428 | -0.428 |
| depre6_o t2 | 0.085  | 0.020 | 4.323   | 0.000 | 0.085  | 0.085  |
| depre6_o t3 | 0.741  | 0.022 | 34.219  | 0.000 | 0.741  | 0.741  |
| depre6_o t4 | 1.255  | 0.026 | 47.633  | 0.000 | 1.255  | 1.255  |

Variances:



# A one-factor categorical CFA model ...

|            | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|------------|----------|---------|---------|---------|--------|---------|
| depress    | 1.000    |         |         |         | 1.000  | 1.000   |
| .depre1_o  | 0.496    |         |         |         | 0.496  | 0.496   |
| .depre2_o  | 0.571    |         |         |         | 0.571  | 0.571   |
| .depre3_o  | 0.446    |         |         |         | 0.446  | 0.446   |
| .depre4_o  | 0.489    |         |         |         | 0.489  | 0.489   |
| .depre5_o  | 0.637    |         |         |         | 0.637  | 0.637   |
| .depre6_o  | 0.653    |         |         |         | 0.653  | 0.653   |
| Scales y*: |          |         |         |         |        |         |
|            | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depre1_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| depre2_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| depre3_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| depre4_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| depre5_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| depre6_o   | 1.000    |         |         |         | 1.000  | 1.000   |

# A three-factor categorical CFA model

```
## Specifying the model-structure object
cfa.04.ord <- '
  gotBully =~ NA*gotBu1_o + gotBu2_o + gotBu3_o +
              gotBu4_o + gotBu5_o + gotBu6_o +
              gotBu7_o + gotBu8_o + gotBu9_o
  gotBully ~ 1*gotBully

  depress =~ NA*depre1_o + depre2_o + depre3_o +
            depre4_o + depre5_o + depre6_o
  depress ~ 1*depress

  alcohol =~ NA*alc1_o + alc2_o + alc3_o +
            alc4_o + alc5_o
  alcohol ~ 1*alcohol '
## Estimating the model
cfa.04.ord.fit <-
  cfa(model = cfa.04.ord, data = hbsc,
```

# A three-factor categorical CFA model ...

```
mimic = "Mplus", estimator = "WLSMV")
## Requesting an estimation summary
summary(cfa.04.ord.fit, fit.measures = TRUE,
        standardized = TRUE)
```

```
lavaan 0.6-3 ended normally after 17 iterations
```

|  |         |          |
|--|---------|----------|
| Optimization method                        | NLMINB  |          |
| Number of free parameters                  | 103     |          |
|  | Used    | Total    |
| Number of observations                     | 2684    | 4284     |
| Estimator                                  | DWLS    | Robust   |
| Model Fit Test Statistic                   | 870.308 | 1046.718 |
| Degrees of freedom                         | 167     | 167      |
| P-value (Chi-square)                       | 0.000   | 0.000    |
| Scaling correction factor                  |         | 0.876    |
| Shift parameter                            |         | 52.908   |
| for simple second-order correction (WLSMV) |         |          |

```
Model test baseline model:
```

# A three-factor categorical CFA model ...

|  |             |           |
|--|-------------|-----------|
| Minimum Function Test Statistic          | 75123.245   | 30297.601 |
| Degrees of freedom                       | 190         | 190       |
| P-value                                  | 0.000       | 0.000     |
| User model versus baseline model:        |             |           |
| Comparative Fit Index (CFI)              | 0.991       | 0.971     |
| Tucker-Lewis Index (TLI)                 | 0.989       | 0.967     |
| Robust Comparative Fit Index (CFI)       |             | NA        |
| Robust Tucker-Lewis Index (TLI)          |             | NA        |
| Root Mean Square Error of Approximation: |             |           |
| RMSEA                                    | 0.040       | 0.044     |
| 90 Percent Confidence Interval           | 0.037 0.042 | 0.042     |
| 0.047                                    |             |           |
| P-value RMSEA <= 0.05                    | 1.000       | 1.000     |
| Robust RMSEA                             |             | NA        |
| 90 Percent Confidence Interval           |             | NA        |
| NA                                       |             |           |
| Standardized Root Mean Square Residual:  |             |           |
| SRMR                                     | 0.052       | 0.052     |

# A three-factor categorical CFA model ...

Weighted Root Mean Square Residual:

|      |       |       |
|------|-------|-------|
| WRMR | 1.795 | 1.795 |
|------|-------|-------|

Parameter Estimates:

|                                  |              |
|----------------------------------|--------------|
| Information                      | Expected     |
| Information saturated (h1) model | Unstructured |
| Standard Errors                  | Robust.sem   |

Latent Variables:

|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-------------|----------|---------|---------|---------|--------|---------|
| gotBully =~ |          |         |         |         |        |         |
| gotBu1_o    | 0.752    | 0.013   | 56.021  | 0.000   | 0.752  | 0.752   |
| gotBu2_o    | 0.780    | 0.013   | 59.261  | 0.000   | 0.780  | 0.780   |
| gotBu3_o    | 0.778    | 0.015   | 53.290  | 0.000   | 0.778  | 0.778   |
| gotBu4_o    | 0.807    | 0.011   | 70.920  | 0.000   | 0.807  | 0.807   |
| gotBu5_o    | 0.840    | 0.012   | 67.419  | 0.000   | 0.840  | 0.840   |
| gotBu6_o    | 0.866    | 0.013   | 65.080  | 0.000   | 0.866  | 0.866   |
| gotBu7_o    | 0.770    | 0.015   | 52.305  | 0.000   | 0.770  | 0.770   |
| gotBu8_o    | 0.861    | 0.014   | 61.460  | 0.000   | 0.861  | 0.861   |
| gotBu9_o    | 0.891    | 0.016   | 57.294  | 0.000   | 0.891  | 0.891   |
| depress =~  |          |         |         |         |        |         |
| depre1_o    | 0.692    | 0.014   | 49.499  | 0.000   | 0.692  | 0.692   |
| depre2_o    | 0.640    | 0.015   | 43.858  | 0.000   | 0.640  | 0.640   |

# A three-factor categorical CFA model ...

|              |          |         |         |         |        |         |
|--------------|----------|---------|---------|---------|--------|---------|
| depre3_o     | 0.753    | 0.015   | 48.958  | 0.000   | 0.753  | 0.753   |
| depre4_o     | 0.710    | 0.015   | 47.969  | 0.000   | 0.710  | 0.710   |
| depre5_o     | 0.597    | 0.017   | 35.102  | 0.000   | 0.597  | 0.597   |
| depre6_o     | 0.628    | 0.016   | 38.109  | 0.000   | 0.628  | 0.628   |
| alcohol =~   |          |         |         |         |        |         |
| alc1_o       | 0.859    | 0.013   | 67.423  | 0.000   | 0.859  | 0.859   |
| alc2_o       | 0.774    | 0.016   | 47.124  | 0.000   | 0.774  | 0.774   |
| alc3_o       | 0.951    | 0.009   | 106.901 | 0.000   | 0.951  | 0.951   |
| alc4_o       | 0.882    | 0.010   | 84.795  | 0.000   | 0.882  | 0.882   |
| alc5_o       | 0.907    | 0.009   | 100.941 | 0.000   | 0.907  | 0.907   |
| Covariances: |          |         |         |         |        |         |
|              | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| gotBully ~   |          |         |         |         |        |         |
| depress      | 0.438    | 0.024   | 18.438  | 0.000   | 0.438  | 0.438   |
| alcohol      | 0.262    | 0.031   | 8.361   | 0.000   | 0.262  | 0.262   |
| depress ~    |          |         |         |         |        |         |
| alcohol      | 0.354    | 0.028   | 12.467  | 0.000   | 0.354  | 0.354   |
| Intercepts:  |          |         |         |         |        |         |
|              | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| .gotBu1_o    | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu2_o    | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu3_o    | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu4_o    | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu5_o    | 0.000    |         |         |         | 0.000  | 0.000   |

# A three-factor categorical CFA model ...

|    |           |       |  |  |       |       |
|----|-----------|-------|--|--|-------|-------|
| 05 | .gotBu6_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .gotBu7_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .gotBu8_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .gotBu9_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .depre1_o | 0.000 |  |  | 0.000 | 0.000 |
| 00 | .depre2_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .depre3_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .depre4_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .depre5_o | 0.000 |  |  | 0.000 | 0.000 |
|    | .depre6_o | 0.000 |  |  | 0.000 | 0.000 |
| 05 | .alc1_o   | 0.000 |  |  | 0.000 | 0.000 |
|    | .alc2_o   | 0.000 |  |  | 0.000 | 0.000 |
|    | .alc3_o   | 0.000 |  |  | 0.000 | 0.000 |
|    | .alc4_o   | 0.000 |  |  | 0.000 | 0.000 |
|    | .alc5_o   | 0.000 |  |  | 0.000 | 0.000 |
|    | gotBully  | 0.000 |  |  | 0.000 | 0.000 |
| 10 | depress   | 0.000 |  |  | 0.000 | 0.000 |
|    | alcohol   | 0.000 |  |  | 0.000 | 0.000 |

## Thresholds :

|    | Estimate    | Std.Err | z-value | P(> z ) | Std.lv | Std.all |       |
|----|-------------|---------|---------|---------|--------|---------|-------|
| 15 | gotBu1_o t1 | 0.266   | 0.025   | 10.870  | 0.000  | 0.266   | 0.266 |
|    | gotBu1_o t2 | 0.852   | 0.028   | 30.781  | 0.000  | 0.852   | 0.852 |
|    | gotBu1_o t3 | 1.070   | 0.030   | 35.696  | 0.000  | 1.070   | 1.070 |
|    | gotBu1_o t4 | 1.319   | 0.034   | 39.208  | 0.000  | 1.319   | 1.319 |
| 20 | gotBu2_o t1 | 0.470   | 0.025   | 18.640  | 0.000  | 0.470   | 0.470 |

# A three-factor categorical CFA model ...

|    |             |       |       |        |       |       |       |
|----|-------------|-------|-------|--------|-------|-------|-------|
|    | gotBu2_o t2 | 1.028 | 0.029 | 34.876 | 0.000 | 1.028 | 1.028 |
|    | gotBu2_o t3 | 1.241 | 0.032 | 38.356 | 0.000 | 1.241 | 1.241 |
|    | gotBu2_o t4 | 1.539 | 0.038 | 40.373 | 0.000 | 1.539 | 1.539 |
| 25 | gotBu3_o t1 | 0.906 | 0.028 | 32.141 | 0.000 | 0.906 | 0.906 |
|    | gotBu3_o t2 | 1.331 | 0.034 | 39.311 | 0.000 | 1.331 | 1.331 |
|    | gotBu3_o t3 | 1.546 | 0.038 | 40.380 | 0.000 | 1.546 | 1.546 |
|    | gotBu3_o t4 | 1.802 | 0.046 | 39.528 | 0.000 | 1.802 | 1.802 |
|    | gotBu4_o t1 | 0.304 | 0.025 | 12.369 | 0.000 | 0.304 | 0.304 |
|    | gotBu4_o t2 | 0.917 | 0.028 | 32.416 | 0.000 | 0.917 | 0.917 |
| 30 | gotBu4_o t3 | 1.204 | 0.032 | 37.867 | 0.000 | 1.204 | 1.204 |
|    | gotBu4_o t4 | 1.459 | 0.036 | 40.154 | 0.000 | 1.459 | 1.459 |
|    | gotBu5_o t1 | 1.012 | 0.029 | 34.554 | 0.000 | 1.012 | 1.012 |
|    | gotBu5_o t2 | 1.375 | 0.035 | 39.672 | 0.000 | 1.375 | 1.375 |
|    | gotBu5_o t3 | 1.555 | 0.038 | 40.388 | 0.000 | 1.555 | 1.555 |
| 35 | gotBu5_o t4 | 1.831 | 0.047 | 39.298 | 0.000 | 1.831 | 1.831 |
|    | gotBu6_o t1 | 1.251 | 0.033 | 38.479 | 0.000 | 1.251 | 1.251 |
|    | gotBu6_o t2 | 1.580 | 0.039 | 40.395 | 0.000 | 1.580 | 1.580 |
|    | gotBu6_o t3 | 1.788 | 0.045 | 39.629 | 0.000 | 1.788 | 1.788 |
|    | gotBu6_o t4 | 2.029 | 0.055 | 37.126 | 0.000 | 2.029 | 2.029 |
| 40 | gotBu7_o t1 | 0.649 | 0.026 | 24.818 | 0.000 | 0.649 | 0.649 |
|    | gotBu7_o t2 | 1.077 | 0.030 | 35.819 | 0.000 | 1.077 | 1.077 |
|    | gotBu7_o t3 | 1.291 | 0.033 | 38.926 | 0.000 | 1.291 | 1.291 |
|    | gotBu7_o t4 | 1.564 | 0.039 | 40.393 | 0.000 | 1.564 | 1.564 |
|    | gotBu8_o t1 | 1.361 | 0.034 | 39.564 | 0.000 | 1.361 | 1.361 |
| 45 | gotBu8_o t2 | 1.695 | 0.042 | 40.149 | 0.000 | 1.695 | 1.695 |
|    | gotBu8_o t3 | 1.889 | 0.049 | 38.768 | 0.000 | 1.889 | 1.889 |



# A three-factor categorical CFA model ...

|             |        |       |         |       |        |        |
|-------------|--------|-------|---------|-------|--------|--------|
| gotBu8_o t4 | 2.083  | 0.057 | 36.366  | 0.000 | 2.083  | 2.083  |
| gotBu9_o t1 | 1.492  | 0.037 | 40.273  | 0.000 | 1.492  | 1.492  |
| gotBu9_o t2 | 1.744  | 0.044 | 39.911  | 0.000 | 1.744  | 1.744  |
| gotBu9_o t3 | 1.889  | 0.049 | 38.768  | 0.000 | 1.889  | 1.889  |
| gotBu9_o t4 | 2.075  | 0.057 | 36.484  | 0.000 | 2.075  | 2.075  |
| depre1_o t1 | -0.553 | 0.026 | -21.595 | 0.000 | -0.553 | -0.553 |
| depre1_o t2 | 0.163  | 0.024 | 6.712   | 0.000 | 0.163  | 0.163  |
| depre1_o t3 | 1.095  | 0.030 | 36.155  | 0.000 | 1.095  | 1.095  |
| depre1_o t4 | 1.812  | 0.046 | 39.455  | 0.000 | 1.812  | 1.812  |
| depre2_o t1 | -0.906 | 0.028 | -32.141 | 0.000 | -0.906 | -0.906 |
| depre2_o t2 | -0.175 | 0.024 | -7.174  | 0.000 | -0.175 | -0.175 |
| depre2_o t3 | 0.749  | 0.027 | 27.912  | 0.000 | 0.749  | 0.749  |
| depre2_o t4 | 1.533  | 0.038 | 40.365  | 0.000 | 1.533  | 1.533  |
| depre3_o t1 | 0.293  | 0.025 | 11.908  | 0.000 | 0.293  | 0.293  |
| depre3_o t2 | 0.687  | 0.026 | 26.041  | 0.000 | 0.687  | 0.687  |
| depre3_o t3 | 1.168  | 0.031 | 37.350  | 0.000 | 1.168  | 1.168  |
| depre3_o t4 | 1.642  | 0.041 | 40.317  | 0.000 | 1.642  | 1.642  |
| depre4_o t1 | -0.152 | 0.024 | -6.249  | 0.000 | -0.152 | -0.152 |
| depre4_o t2 | 0.247  | 0.024 | 10.101  | 0.000 | 0.247  | 0.247  |
| depre4_o t3 | 0.897  | 0.028 | 31.934  | 0.000 | 0.897  | 0.897  |
| depre4_o t4 | 1.478  | 0.037 | 40.228  | 0.000 | 1.478  | 1.478  |
| depre5_o t1 | -0.410 | 0.025 | -16.429 | 0.000 | -0.410 | -0.410 |
| depre5_o t2 | 0.053  | 0.024 | 2.200   | 0.028 | 0.053  | 0.053  |
| depre5_o t3 | 0.656  | 0.026 | 25.041  | 0.000 | 0.656  | 0.656  |
| depre5_o t4 | 1.237  | 0.032 | 38.306  | 0.000 | 1.237  | 1.237  |
| depre6_o t1 | -0.454 | 0.025 | -18.069 | 0.000 | -0.454 | -0.454 |

# A three-factor categorical CFA model ...

|             |       |       |        |       |       |       |
|-------------|-------|-------|--------|-------|-------|-------|
| depre6_o t2 | 0.092 | 0.024 | 3.781  | 0.000 | 0.092 | 0.092 |
| depre6_o t3 | 0.733 | 0.027 | 27.438 | 0.000 | 0.733 | 0.733 |
| depre6_o t4 | 1.261 | 0.033 | 38.600 | 0.000 | 1.261 | 1.261 |
| alc1_o t1   | 1.060 | 0.030 | 35.509 | 0.000 | 1.060 | 1.060 |
| alc1_o t2   | 1.836 | 0.047 | 39.256 | 0.000 | 1.836 | 1.836 |
| alc1_o t3   | 2.193 | 0.063 | 34.638 | 0.000 | 2.193 | 2.193 |
| alc1_o t4   | 2.435 | 0.081 | 30.190 | 0.000 | 2.435 | 2.435 |
| alc2_o t1   | 0.927 | 0.028 | 32.655 | 0.000 | 0.927 | 0.927 |
| alc2_o t2   | 1.816 | 0.046 | 39.417 | 0.000 | 1.816 | 1.816 |
| alc2_o t3   | 2.117 | 0.059 | 35.858 | 0.000 | 2.117 | 2.117 |
| alc2_o t4   | 2.473 | 0.084 | 29.438 | 0.000 | 2.473 | 2.473 |
| alc3_o t1   | 1.317 | 0.034 | 39.187 | 0.000 | 1.317 | 1.317 |
| alc3_o t2   | 1.816 | 0.046 | 39.417 | 0.000 | 1.816 | 1.816 |
| alc3_o t3   | 2.075 | 0.057 | 36.484 | 0.000 | 2.075 | 2.075 |
| alc3_o t4   | 2.435 | 0.081 | 30.190 | 0.000 | 2.435 | 2.435 |
| alc4_o t1   | 0.983 | 0.029 | 33.932 | 0.000 | 0.983 | 0.983 |
| alc4_o t2   | 1.604 | 0.040 | 40.381 | 0.000 | 1.604 | 1.604 |
| alc4_o t3   | 2.000 | 0.053 | 37.499 | 0.000 | 2.000 | 2.000 |
| alc4_o t4   | 2.353 | 0.074 | 31.773 | 0.000 | 2.353 | 2.353 |
| alc5_o t1   | 1.067 | 0.030 | 35.633 | 0.000 | 1.067 | 1.067 |
| alc5_o t2   | 1.719 | 0.043 | 40.042 | 0.000 | 1.719 | 1.719 |
| alc5_o t3   | 2.036 | 0.055 | 37.026 | 0.000 | 2.036 | 2.036 |
| alc5_o t4   | 2.353 | 0.074 | 31.773 | 0.000 | 2.353 | 2.353 |

Variances:

| Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|---------|---------|---------|--------|---------|
|----------|---------|---------|---------|--------|---------|

# A three-factor categorical CFA model ...

|           |       |  |  |       |       |
|-----------|-------|--|--|-------|-------|
| gotBully  | 1.000 |  |  | 1.000 | 1.000 |
| depress   | 1.000 |  |  | 1.000 | 1.000 |
| alcohol   | 1.000 |  |  | 1.000 | 1.000 |
| .gotBu1_o | 0.435 |  |  | 0.435 | 0.435 |
| .gotBu2_o | 0.391 |  |  | 0.391 | 0.391 |
| .gotBu3_o | 0.395 |  |  | 0.395 | 0.395 |
| .gotBu4_o | 0.348 |  |  | 0.348 | 0.348 |
| .gotBu5_o | 0.295 |  |  | 0.295 | 0.295 |
| .gotBu6_o | 0.249 |  |  | 0.249 | 0.249 |
| .gotBu7_o | 0.407 |  |  | 0.407 | 0.407 |
| .gotBu8_o | 0.259 |  |  | 0.259 | 0.259 |
| .gotBu9_o | 0.206 |  |  | 0.206 | 0.206 |
| .depre1_o | 0.521 |  |  | 0.521 | 0.521 |
| .depre2_o | 0.591 |  |  | 0.591 | 0.591 |
| .depre3_o | 0.432 |  |  | 0.432 | 0.432 |
| .depre4_o | 0.495 |  |  | 0.495 | 0.495 |
| .depre5_o | 0.643 |  |  | 0.643 | 0.643 |
| .depre6_o | 0.606 |  |  | 0.606 | 0.606 |
| .alc1_o   | 0.262 |  |  | 0.262 | 0.262 |
| .alc2_o   | 0.401 |  |  | 0.401 | 0.401 |
| .alc3_o   | 0.095 |  |  | 0.095 | 0.095 |
| .alc4_o   | 0.221 |  |  | 0.221 | 0.221 |
| .alc5_o   | 0.178 |  |  | 0.178 | 0.178 |

Scales y\*:

| Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|---------|---------|---------|--------|---------|
|----------|---------|---------|---------|--------|---------|

# A three-factor categorical CFA model ...

|    |          |       |       |       |
|----|----------|-------|-------|-------|
| 25 | gotBu1_o | 1.000 | 1.000 | 1.000 |
|    | gotBu2_o | 1.000 | 1.000 | 1.000 |
|    | gotBu3_o | 1.000 | 1.000 | 1.000 |
|    | gotBu4_o | 1.000 | 1.000 | 1.000 |
|    | gotBu5_o | 1.000 | 1.000 | 1.000 |
| 30 | gotBu6_o | 1.000 | 1.000 | 1.000 |
|    | gotBu7_o | 1.000 | 1.000 | 1.000 |
|    | gotBu8_o | 1.000 | 1.000 | 1.000 |
|    | gotBu9_o | 1.000 | 1.000 | 1.000 |
|    | depre1_o | 1.000 | 1.000 | 1.000 |
| 35 | depre2_o | 1.000 | 1.000 | 1.000 |
|    | depre3_o | 1.000 | 1.000 | 1.000 |
|    | depre4_o | 1.000 | 1.000 | 1.000 |
|    | depre5_o | 1.000 | 1.000 | 1.000 |
|    | depre6_o | 1.000 | 1.000 | 1.000 |
| 40 | alc1_o   | 1.000 | 1.000 | 1.000 |
|    | alc2_o   | 1.000 | 1.000 | 1.000 |
|    | alc3_o   | 1.000 | 1.000 | 1.000 |
|    | alc4_o   | 1.000 | 1.000 | 1.000 |
|    | alc5_o   | 1.000 | 1.000 | 1.000 |

# Outline

- 1 Two Meanings of Non-Normality
- 2 Should Ordinal Data Be Treated as Numeric Data?
  - Current common practices
  - Ordinal data should be modeled differently
  - Ordinal data can be treated as numeric (with caution!)
- 3 Estimators for categorical data
- 4 CFA Models with Ordinal Data
  - Data input/type
  - CFA Models with Ordinal Data from HBSC
- 5 Structural Models with Ordinal Data
  - Direct regressive models
  - Indirect effect (mediation) models
- 6 Measurement Invariance Testing with Ordinal Data

# A structural model with ordinal indicators

```
## Specifying the model-structure object
sem.01.ord <- '
  gotBully =~ NA*gotBu1_o + gotBu2_o + gotBu3_o +
              gotBu4_o + gotBu5_o + gotBu6_o +
              gotBu7_o + gotBu8_o + gotBu9_o
  gotBully ~ 1*gotBully

  alcohol =~ NA*alc1_o + alc2_o + alc3_o +
            alc4_o + alc5_o
  alcohol ~ 1*alcohol

  alcohol ~ gotBully '
## Estimating the model
sem.01.ord.fit <-
  sem(model = sem.01.ord, data = hbsc,
      mimic = "Mplus", estimator = "WLSMV")
## Requesting an estimation summary
```

# A structural model with ordinal indicators ...

```
summary(sem.01.ord.fit, fit.measures = TRUE,
        standardized = TRUE)
```

```
lavaan 0.6-3 ended normally after 22 iterations
```

|  |         |         |
|--|---------|---------|
| Optimization method                        | NLMINB  |         |
| Number of free parameters                  | 71      |         |
|  | Used    | Total   |
| Number of observations                     | 2745    | 4284    |
| Estimator                                  | DWLS    | Robust  |
| Model Fit Test Statistic                   | 491.935 | 646.904 |
| Degrees of freedom                         | 76      | 76      |
| P-value (Chi-square)                       | 0.000   | 0.000   |
| Scaling correction factor                  |         | 0.789   |
| Shift parameter                            |         | 23.365  |
| for simple second-order correction (WLSMV) |         |         |

```
Model test baseline model:
```

|                                 |           |           |
|---------------------------------|-----------|-----------|
| Minimum Function Test Statistic | 61631.106 | 23861.747 |
| Degrees of freedom              | 91        | 91        |
| P-value                         | 0.000     | 0.000     |

# A structural model with ordinal indicators ...

User model versus baseline model:

|                             |       |       |
|-----------------------------|-------|-------|
| Comparative Fit Index (CFI) | 0.993 | 0.976 |
| Tucker-Lewis Index (TLI)    | 0.992 | 0.971 |

|                                    |  |    |
|------------------------------------|--|----|
| Robust Comparative Fit Index (CFI) |  | NA |
| Robust Tucker-Lewis Index (TLI)    |  | NA |

Root Mean Square Error of Approximation:

|                                |       |       |       |
|--------------------------------|-------|-------|-------|
| RMSEA                          |       | 0.045 | 0.052 |
| 90 Percent Confidence Interval | 0.041 | 0.048 | 0.049 |
| 0.056                          |       |       |       |

|                           |  |       |       |
|---------------------------|--|-------|-------|
| P-value RMSEA $\leq$ 0.05 |  | 0.990 | 0.148 |
|---------------------------|--|-------|-------|

|                                |  |  |    |
|--------------------------------|--|--|----|
| Robust RMSEA                   |  |  | NA |
| 90 Percent Confidence Interval |  |  | NA |
| NA                             |  |  |    |

Standardized Root Mean Square Residual:

|      |  |       |       |
|------|--|-------|-------|
| SRMR |  | 0.057 | 0.057 |
|------|--|-------|-------|

Weighted Root Mean Square Residual:



# A structural model with ordinal indicators ...

| WRMR                             |          | 1.829   | 1.829   |              |        |         |
|----------------------------------|----------|---------|---------|--------------|--------|---------|
| Parameter Estimates:             |          |         |         |              |        |         |
| Information                      |          |         |         | Expected     |        |         |
| Information saturated (h1) model |          |         |         | Unstructured |        |         |
| Standard Errors                  |          |         |         | Robust.sem   |        |         |
| Latent Variables:                |          |         |         |              |        |         |
|                                  | Estimate | Std.Err | z-value | P(> z )      | Std.lv | Std.all |
| gotBully =~                      |          |         |         |              |        |         |
| gotBu1_o                         | 0.745    | 0.013   | 55.379  | 0.000        | 0.745  | 0.745   |
| gotBu2_o                         | 0.774    | 0.013   | 59.107  | 0.000        | 0.774  | 0.774   |
| gotBu3_o                         | 0.790    | 0.014   | 56.927  | 0.000        | 0.790  | 0.790   |
| gotBu4_o                         | 0.798    | 0.011   | 71.210  | 0.000        | 0.798  | 0.798   |
| gotBu5_o                         | 0.842    | 0.012   | 70.209  | 0.000        | 0.842  | 0.842   |
| gotBu6_o                         | 0.879    | 0.012   | 70.731  | 0.000        | 0.879  | 0.879   |
| gotBu7_o                         | 0.762    | 0.014   | 53.164  | 0.000        | 0.762  | 0.762   |
| gotBu8_o                         | 0.874    | 0.013   | 66.741  | 0.000        | 0.874  | 0.874   |
| gotBu9_o                         | 0.905    | 0.014   | 62.407  | 0.000        | 0.905  | 0.905   |
| alcohol =~                       |          |         |         |              |        |         |
| alc1_o                           | 0.833    | 0.013   | 62.215  | 0.000        | 0.867  | 0.867   |
| alc2_o                           | 0.757    | 0.016   | 47.938  | 0.000        | 0.788  | 0.788   |
| alc3_o                           | 0.912    | 0.011   | 82.275  | 0.000        | 0.949  | 0.949   |
| alc4_o                           | 0.846    | 0.012   | 70.018  | 0.000        | 0.881  | 0.881   |
| alc5_o                           | 0.871    | 0.012   | 74.238  | 0.000        | 0.906  | 0.906   |

# A structural model with ordinal indicators ...

| Regressions:          |          |         |         |         |        |         |
|-----------------------|----------|---------|---------|---------|--------|---------|
|                       | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| alcohol ~<br>gotBully | 0.289    | 0.035   | 8.370   | 0.000   | 0.278  | 0.278   |
| Intercepts:           |          |         |         |         |        |         |
|                       | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| .gotBu1_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu2_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu3_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu4_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu5_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu6_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu7_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu8_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .gotBu9_o             | 0.000    |         |         |         | 0.000  | 0.000   |
| .alc1_o               | 0.000    |         |         |         | 0.000  | 0.000   |
| .alc2_o               | 0.000    |         |         |         | 0.000  | 0.000   |
| .alc3_o               | 0.000    |         |         |         | 0.000  | 0.000   |
| .alc4_o               | 0.000    |         |         |         | 0.000  | 0.000   |
| .alc5_o               | 0.000    |         |         |         | 0.000  | 0.000   |
| gotBully              | 0.000    |         |         |         | 0.000  | 0.000   |
| .alcohol              | 0.000    |         |         |         | 0.000  | 0.000   |
| Thresholds:           |          |         |         |         |        |         |

# A structural model with ordinal indicators ...

|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-------------|----------|---------|---------|---------|--------|---------|
| gotBu1_o t1 | 0.272    | 0.024   | 11.224  | 0.000   | 0.272  | 0.272   |
| gotBu1_o t2 | 0.853    | 0.027   | 31.165  | 0.000   | 0.853  | 0.853   |
| gotBu1_o t3 | 1.066    | 0.030   | 36.028  | 0.000   | 1.066  | 1.066   |
| gotBu1_o t4 | 1.321    | 0.033   | 39.666  | 0.000   | 1.321  | 1.321   |
| gotBu2_o t1 | 0.473    | 0.025   | 18.982  | 0.000   | 0.473  | 0.473   |
| gotBu2_o t2 | 1.028    | 0.029   | 35.279  | 0.000   | 1.028  | 1.028   |
| gotBu2_o t3 | 1.242    | 0.032   | 38.803  | 0.000   | 1.242  | 1.242   |
| gotBu2_o t4 | 1.542    | 0.038   | 40.832  | 0.000   | 1.542  | 1.542   |
| gotBu3_o t1 | 0.902    | 0.028   | 32.407  | 0.000   | 0.902  | 0.902   |
| gotBu3_o t2 | 1.323    | 0.033   | 39.687  | 0.000   | 1.323  | 1.323   |
| gotBu3_o t3 | 1.539    | 0.038   | 40.829  | 0.000   | 1.539  | 1.539   |
| gotBu3_o t4 | 1.803    | 0.045   | 39.968  | 0.000   | 1.803  | 1.803   |
| gotBu4_o t1 | 0.305    | 0.024   | 12.516  | 0.000   | 0.305  | 0.305   |
| gotBu4_o t2 | 0.914    | 0.028   | 32.713  | 0.000   | 0.914  | 0.914   |
| gotBu4_o t3 | 1.200    | 0.031   | 38.242  | 0.000   | 1.200  | 1.200   |
| gotBu4_o t4 | 1.460    | 0.036   | 40.613  | 0.000   | 1.460  | 1.460   |
| gotBu5_o t1 | 1.007    | 0.029   | 34.832  | 0.000   | 1.007  | 1.007   |
| gotBu5_o t2 | 1.373    | 0.034   | 40.106  | 0.000   | 1.373  | 1.373   |
| gotBu5_o t3 | 1.551    | 0.038   | 40.842  | 0.000   | 1.551  | 1.551   |
| gotBu5_o t4 | 1.831    | 0.046   | 39.740  | 0.000   | 1.831  | 1.831   |
| gotBu6_o t1 | 1.250    | 0.032   | 38.900  | 0.000   | 1.250  | 1.250   |
| gotBu6_o t2 | 1.572    | 0.038   | 40.852  | 0.000   | 1.572  | 1.572   |
| gotBu6_o t3 | 1.785    | 0.045   | 40.101  | 0.000   | 1.785  | 1.785   |
| gotBu6_o t4 | 2.024    | 0.054   | 37.614  | 0.000   | 2.024  | 2.024   |
| gotBu7_o t1 | 0.651    | 0.026   | 25.163  | 0.000   | 0.651  | 0.651   |

# A structural model with ordinal indicators ...

|             |       |       |        |       |       |       |
|-------------|-------|-------|--------|-------|-------|-------|
| gotBu7_o t2 | 1.079 | 0.030 | 36.272 | 0.000 | 1.079 | 1.079 |
| gotBu7_o t3 | 1.293 | 0.033 | 39.388 | 0.000 | 1.293 | 1.293 |
| gotBu7_o t4 | 1.572 | 0.038 | 40.852 | 0.000 | 1.572 | 1.572 |
| gotBu8_o t1 | 1.359 | 0.034 | 39.998 | 0.000 | 1.359 | 1.359 |
| gotBu8_o t2 | 1.682 | 0.041 | 40.652 | 0.000 | 1.682 | 1.682 |
| gotBu8_o t3 | 1.872 | 0.048 | 39.375 | 0.000 | 1.872 | 1.872 |
| gotBu8_o t4 | 2.061 | 0.056 | 37.103 | 0.000 | 2.061 | 2.061 |
| gotBu9_o t1 | 1.484 | 0.036 | 40.704 | 0.000 | 1.484 | 1.484 |
| gotBu9_o t2 | 1.737 | 0.043 | 40.397 | 0.000 | 1.737 | 1.737 |
| gotBu9_o t3 | 1.877 | 0.048 | 39.324 | 0.000 | 1.877 | 1.877 |
| gotBu9_o t4 | 2.076 | 0.056 | 36.878 | 0.000 | 2.076 | 2.076 |
| alc1_o t1   | 1.063 | 0.030 | 35.966 | 0.000 | 1.063 | 1.063 |
| alc1_o t2   | 1.822 | 0.046 | 39.820 | 0.000 | 1.822 | 1.822 |
| alc1_o t3   | 2.172 | 0.061 | 35.382 | 0.000 | 2.172 | 2.172 |
| alc1_o t4   | 2.392 | 0.076 | 31.376 | 0.000 | 2.392 | 2.392 |
| alc2_o t1   | 0.924 | 0.028 | 32.950 | 0.000 | 0.924 | 0.924 |
| alc2_o t2   | 1.808 | 0.045 | 39.933 | 0.000 | 1.808 | 1.808 |
| alc2_o t3   | 2.100 | 0.058 | 36.516 | 0.000 | 2.100 | 2.100 |
| alc2_o t4   | 2.443 | 0.080 | 30.370 | 0.000 | 2.443 | 2.443 |
| alc3_o t1   | 1.314 | 0.033 | 39.604 | 0.000 | 1.314 | 1.314 |
| alc3_o t2   | 1.812 | 0.045 | 39.896 | 0.000 | 1.812 | 1.812 |
| alc3_o t3   | 2.068 | 0.056 | 36.992 | 0.000 | 2.068 | 2.068 |
| alc3_o t4   | 2.425 | 0.079 | 30.721 | 0.000 | 2.425 | 2.425 |
| alc4_o t1   | 0.987 | 0.029 | 34.411 | 0.000 | 0.987 | 0.987 |
| alc4_o t2   | 1.601 | 0.039 | 40.840 | 0.000 | 1.601 | 1.601 |
| alc4_o t3   | 1.990 | 0.052 | 38.061 | 0.000 | 1.990 | 1.990 |

# A structural model with ordinal indicators ...

|    |            |          |         |         |         |        |         |
|----|------------|----------|---------|---------|---------|--------|---------|
| 50 | alc4_o t4  | 2.319    | 0.071   | 32.776  | 0.000   | 2.319  | 2.319   |
|    | alc5_o t1  | 1.068    | 0.030   | 36.059  | 0.000   | 1.068  | 1.068   |
|    | alc5_o t2  | 1.717    | 0.042   | 40.503  | 0.000   | 1.717  | 1.717   |
|    | alc5_o t3  | 2.031    | 0.054   | 37.517  | 0.000   | 2.031  | 2.031   |
|    | alc5_o t4  | 2.347    | 0.073   | 32.252  | 0.000   | 2.347  | 2.347   |
| 55 | Variances: |          |         |         |         |        |         |
|    |            | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|    | gotBully   | 1.000    |         |         |         | 1.000  | 1.000   |
|    | .alcohol   | 1.000    |         |         |         | 0.923  | 0.923   |
| 50 | .gotBu1_o  | 0.445    |         |         |         | 0.445  | 0.445   |
|    | .gotBu2_o  | 0.401    |         |         |         | 0.401  | 0.401   |
|    | .gotBu3_o  | 0.375    |         |         |         | 0.375  | 0.375   |
|    | .gotBu4_o  | 0.364    |         |         |         | 0.364  | 0.364   |
|    | .gotBu5_o  | 0.292    |         |         |         | 0.292  | 0.292   |
| 55 | .gotBu6_o  | 0.227    |         |         |         | 0.227  | 0.227   |
|    | .gotBu7_o  | 0.420    |         |         |         | 0.420  | 0.420   |
|    | .gotBu8_o  | 0.236    |         |         |         | 0.236  | 0.236   |
|    | .gotBu9_o  | 0.181    |         |         |         | 0.181  | 0.181   |
|    | .alc1_o    | 0.248    |         |         |         | 0.248  | 0.248   |
| 70 | .alc2_o    | 0.380    |         |         |         | 0.380  | 0.380   |
|    | .alc3_o    | 0.100    |         |         |         | 0.100  | 0.100   |
|    | .alc4_o    | 0.225    |         |         |         | 0.225  | 0.225   |
|    | .alc5_o    | 0.178    |         |         |         | 0.178  | 0.178   |
| 75 | Scales y*: |          |         |         |         |        |         |

# A structural model with ordinal indicators ...

|          | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|----------|---------|---------|---------|--------|---------|
| gotBu1_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu2_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu3_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu4_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu5_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu6_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu7_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu8_o | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu9_o | 1.000    |         |         |         | 1.000  | 1.000   |
| alc1_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| alc2_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| alc3_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| alc4_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| alc5_o   | 1.000    |         |         |         | 1.000  | 1.000   |

# An indirect effect model with ordinal data

- Nboot = 10 in order to save time; raise that to 1000 or 2000 in a real project.

```
## Specifying the model-structure object
sem.02.ord <- '
## the measurement model
gotBully =~ NA*gotBu1_o + gotBu2_o + gotBu3_o +
            gotBu4_o + gotBu5_o + gotBu6_o +
            gotBu7_o + gotBu8_o + gotBu9_o
gotBully ~ 1*gotBully

depress =~ NA*depre1_o + depre2_o + depre3_o +
           depre4_o + depre5_o + depre6_o
depress ~ 1*depress

alcohol =~ NA*alc1_o + alc2_o + alc3_o +
           alc4_o + alc5_o
```

# An indirect effect model with ordinal data ...

```
15 alcohol ~ 1*alcohol

## the structural model
## direct effect (the c path)
alcohol ~ c*gotBully

20 ## mediator paths (the a and b path)
## the a path - IV predicting ME
depress ~ a*gotBully
## the b path - ME predicting DV
25 alcohol ~ b*depress

## indirect effect (a*b)
## := operator defines new parameters
ab := a*b

30 ## total effect
```



# An indirect effect model with ordinal data ...

```
total := c + (a*b) '  
## Estimating the model  
Nboot <- 10  
sem.02.ord.fit <-  
  sem(model = sem.02.ord, data = hbosc,  
      mimic = "Mplus", estimator = "DWLS",  
      se = "bootstrap", verbose = TRUE,  
      bootstrap = Nboot)
```

```
Estimating sample thresholds and correlations ... done  
Quasi-Newton steps using NLMINB:  
Objective function = 1.6304782003700506  
Objective function = 4.3078918147412253  
Objective function = 0.5235747582570333  
Objective function = 0.4648468857015091  
Objective function = 0.2962602988611805  
Objective function = 0.5158296626795964  
Objective function = 0.1797810390781590  
Objective function = 0.1794633005086383  
Objective function = 0.1639437760851136  
Objective function = 0.1646792256203331
```

# An indirect effect model with ordinal data ...

```
Objective function = 0.1643922647221566
Objective function = 0.1631750765883284
Objective function = 0.1627453483523332
15 Objective function = 0.1623158721478513
Objective function = 0.1623687520295372
Objective function = 0.1623792467402424
Objective function = 0.1622108420797628
20 Objective function = 0.1621514247023866
Objective function = 0.1621324780354752
Objective function = 0.1621388401677114
Objective function = 0.1621310484748160
Objective function = 0.1621297446938101
25 Objective function = 0.1621298352766599
Objective function = 0.1621290450479564
Objective function = 0.1621291173392306
Objective function = 0.1621289404154801
Objective function = 0.1621289056118569
30 Objective function = 0.1621289055046326
Objective function = 0.1621288871349046
Objective function = 0.1621288847249472
Objective function = 0.1621288850714017
Objective function = 0.1621288845983513
35 Objective function = 0.1621288845924740
Objective function = 0.1621288845727410
Objective function = 0.1621288845793785
Objective function = 0.1621288845727410
```

# An indirect effect model with ordinal data ...

```
convergence status (0=ok): 0
nlminb message says: relative convergence (4)
number of iterations: 24
number of function evaluations [objective, gradient]: 35 24
Computing VCOV for se = bootstrap ...
... bootstrap draw number: 1 OK -- niter = 31 fx =
  0.209263023
... bootstrap draw number: 2 OK -- niter = 31 fx =
  0.187160838
... bootstrap draw number: 3 OK -- niter = 29 fx =
  0.210081105
... bootstrap draw number: 4 OK -- niter = 36 fx =
  0.162921807
... bootstrap draw number: 5 OK -- niter = 30 fx =
  0.191199095
... bootstrap draw number: 6 OK -- niter = 27 fx =
  0.199532107
... bootstrap draw number: 7 OK -- niter = 26 fx =
  0.173135581
... bootstrap draw number: 8 OK -- niter = 28 fx =
  0.195254339
... bootstrap draw number: 9 OK -- niter = 29 fx =
  0.170001213
... bootstrap draw number: 10 OK -- niter = 28 fx =
  0.175450263
Number of successful bootstrap draws: 10
```

# An indirect effect model with ordinal data ...

```
55 done.
Computing TEST for test = standard ... done.
```

```
## Requesting an estimation summary
summary(sem.02.ord.fit, fit.measures = TRUE,
        standardized = TRUE)
```

```
lavaan 0.6-3 ended normally after 24 iterations
```

|                           |         |       |
|---------------------------|---------|-------|
| Optimization method       | NLMINB  |       |
| Number of free parameters | 103     |       |
|                           | Used    | Total |
| Number of observations    | 2684    | 4284  |
| Estimator                 | DWLS    |       |
| Model Fit Test Statistic  | 870.308 |       |
| Degrees of freedom        | 167     |       |
| P-value (Chi-square)      | 0.000   |       |

```
Model test baseline model:
```

|                                 |           |
|---------------------------------|-----------|
| Minimum Function Test Statistic | 75123.245 |
|---------------------------------|-----------|

# An indirect effect model with ordinal data ...

```

Degrees of freedom                190
P-value                          0.000

20 User model versus baseline model:

Comparative Fit Index (CFI)      0.991
Tucker-Lewis Index (TLI)        0.989

25 Root Mean Square Error of Approximation:

RMSEA                            0.040
90 Percent Confidence Interval    0.037 0.042
P-value RMSEA <= 0.05           1.000

30 Standardized Root Mean Square Residual:

SRMR                             0.052

35 Weighted Root Mean Square Residual:

WRMR                             1.795

40 Parameter Estimates:

Standard Errors                   Bootstrap
Number of requested bootstrap draws 10

```

# An indirect effect model with ordinal data ...

Number of successful bootstrap draws

10

Latent Variables:

|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-------------|----------|---------|---------|---------|--------|---------|
| gotBully =~ |          |         |         |         |        |         |
| gotBu1_o    | 0.752    | 0.016   | 45.589  | 0.000   | 0.752  | 0.752   |
| gotBu2_o    | 0.780    | 0.007   | 114.820 | 0.000   | 0.780  | 0.780   |
| gotBu3_o    | 0.778    | 0.018   | 43.671  | 0.000   | 0.778  | 0.778   |
| gotBu4_o    | 0.807    | 0.013   | 60.192  | 0.000   | 0.807  | 0.807   |
| gotBu5_o    | 0.840    | 0.012   | 69.129  | 0.000   | 0.840  | 0.840   |
| gotBu6_o    | 0.866    | 0.015   | 56.432  | 0.000   | 0.866  | 0.866   |
| gotBu7_o    | 0.770    | 0.014   | 55.174  | 0.000   | 0.770  | 0.770   |
| gotBu8_o    | 0.861    | 0.016   | 53.892  | 0.000   | 0.861  | 0.861   |
| gotBu9_o    | 0.891    | 0.014   | 64.221  | 0.000   | 0.891  | 0.891   |
| depress =~  |          |         |         |         |        |         |
| depre1_o    | 0.622    | 0.010   | 64.389  | 0.000   | 0.692  | 0.692   |
| depre2_o    | 0.575    | 0.009   | 62.699  | 0.000   | 0.640  | 0.640   |
| depre3_o    | 0.677    | 0.014   | 50.119  | 0.000   | 0.753  | 0.753   |
| depre4_o    | 0.639    | 0.021   | 30.132  | 0.000   | 0.710  | 0.710   |
| depre5_o    | 0.537    | 0.025   | 21.239  | 0.000   | 0.597  | 0.597   |
| depre6_o    | 0.564    | 0.013   | 42.330  | 0.000   | 0.628  | 0.628   |
| alcohol =~  |          |         |         |         |        |         |
| alc1_o      | 0.797    | 0.016   | 49.334  | 0.000   | 0.859  | 0.859   |
| alc2_o      | 0.718    | 0.013   | 56.980  | 0.000   | 0.774  | 0.774   |
| alc3_o      | 0.883    | 0.014   | 64.691  | 0.000   | 0.951  | 0.951   |
| alc4_o      | 0.819    | 0.016   | 51.826  | 0.000   | 0.882  | 0.882   |

## An indirect effect model with ordinal data ...

|    |              |     |          |         |         |         |        |         |
|----|--------------|-----|----------|---------|---------|---------|--------|---------|
|    | alc5_o       |     | 0.841    | 0.012   | 68.294  | 0.000   | 0.907  | 0.907   |
| 70 | Regressions: |     |          |         |         |         |        |         |
|    |              |     | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|    | alcohol ~    |     |          |         |         |         |        |         |
|    | gotBully     | (c) | 0.143    | 0.047   | 3.036   | 0.002   | 0.133  | 0.133   |
| 75 | depress ~    |     |          |         |         |         |        |         |
|    | gotBully     | (a) | 0.487    | 0.040   | 12.314  | 0.000   | 0.438  | 0.438   |
|    | alcohol ~    |     |          |         |         |         |        |         |
|    | depress      | (b) | 0.286    | 0.053   | 5.367   | 0.000   | 0.295  | 0.295   |
| 80 | Intercepts:  |     |          |         |         |         |        |         |
|    |              |     | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|    | .gotBu1_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .gotBu2_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .gotBu3_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
| 85 | .gotBu4_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .gotBu5_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .gotBu6_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .gotBu7_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .gotBu8_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
| 90 | .gotBu9_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre1_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre2_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre3_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre4_o    |     | 0.000    |         |         |         | 0.000  | 0.000   |

## An indirect effect model with ordinal data ...

|           |       |  |  |       |       |
|-----------|-------|--|--|-------|-------|
| .depre5_o | 0.000 |  |  | 0.000 | 0.000 |
| .depre6_o | 0.000 |  |  | 0.000 | 0.000 |
| .alc1_o   | 0.000 |  |  | 0.000 | 0.000 |
| .alc2_o   | 0.000 |  |  | 0.000 | 0.000 |
| .alc3_o   | 0.000 |  |  | 0.000 | 0.000 |
| .alc4_o   | 0.000 |  |  | 0.000 | 0.000 |
| .alc5_o   | 0.000 |  |  | 0.000 | 0.000 |
| gotBully  | 0.000 |  |  | 0.000 | 0.000 |
| .depress  | 0.000 |  |  | 0.000 | 0.000 |
| .alcohol  | 0.000 |  |  | 0.000 | 0.000 |

## Thresholds :

|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-------------|----------|---------|---------|---------|--------|---------|
| gotBu1_o t1 | 0.266    | 0.024   | 11.129  | 0.000   | 0.266  | 0.266   |
| gotBu1_o t2 | 0.852    | 0.025   | 33.712  | 0.000   | 0.852  | 0.852   |
| gotBu1_o t3 | 1.070    | 0.040   | 26.959  | 0.000   | 1.070  | 1.070   |
| gotBu1_o t4 | 1.319    | 0.047   | 27.952  | 0.000   | 1.319  | 1.319   |
| gotBu2_o t1 | 0.470    | 0.021   | 21.969  | 0.000   | 0.470  | 0.470   |
| gotBu2_o t2 | 1.028    | 0.018   | 57.123  | 0.000   | 1.028  | 1.028   |
| gotBu2_o t3 | 1.241    | 0.020   | 63.134  | 0.000   | 1.241  | 1.241   |
| gotBu2_o t4 | 1.539    | 0.034   | 45.853  | 0.000   | 1.539  | 1.539   |
| gotBu3_o t1 | 0.906    | 0.031   | 29.072  | 0.000   | 0.906  | 0.906   |
| gotBu3_o t2 | 1.331    | 0.036   | 37.065  | 0.000   | 1.331  | 1.331   |
| gotBu3_o t3 | 1.546    | 0.041   | 37.896  | 0.000   | 1.546  | 1.546   |
| gotBu3_o t4 | 1.802    | 0.046   | 38.771  | 0.000   | 1.802  | 1.802   |
| gotBu4_o t1 | 0.304    | 0.015   | 20.290  | 0.000   | 0.304  | 0.304   |



# An indirect effect model with ordinal data ...

|             |        |       |         |       |        |        |
|-------------|--------|-------|---------|-------|--------|--------|
| gotBu4_o t2 | 0.917  | 0.021 | 42.775  | 0.000 | 0.917  | 0.917  |
| gotBu4_o t3 | 1.204  | 0.040 | 30.099  | 0.000 | 1.204  | 1.204  |
| gotBu4_o t4 | 1.459  | 0.031 | 47.584  | 0.000 | 1.459  | 1.459  |
| gotBu5_o t1 | 1.012  | 0.044 | 22.826  | 0.000 | 1.012  | 1.012  |
| gotBu5_o t2 | 1.375  | 0.041 | 33.501  | 0.000 | 1.375  | 1.375  |
| gotBu5_o t3 | 1.555  | 0.053 | 29.501  | 0.000 | 1.555  | 1.555  |
| gotBu5_o t4 | 1.831  | 0.050 | 36.635  | 0.000 | 1.831  | 1.831  |
| gotBu6_o t1 | 1.251  | 0.045 | 28.081  | 0.000 | 1.251  | 1.251  |
| gotBu6_o t2 | 1.580  | 0.053 | 29.793  | 0.000 | 1.580  | 1.580  |
| gotBu6_o t3 | 1.788  | 0.058 | 30.879  | 0.000 | 1.788  | 1.788  |
| gotBu6_o t4 | 2.029  | 0.051 | 39.506  | 0.000 | 2.029  | 2.029  |
| gotBu7_o t1 | 0.649  | 0.037 | 17.614  | 0.000 | 0.649  | 0.649  |
| gotBu7_o t2 | 1.077  | 0.025 | 43.744  | 0.000 | 1.077  | 1.077  |
| gotBu7_o t3 | 1.291  | 0.022 | 57.465  | 0.000 | 1.291  | 1.291  |
| gotBu7_o t4 | 1.564  | 0.026 | 59.079  | 0.000 | 1.564  | 1.564  |
| gotBu8_o t1 | 1.361  | 0.023 | 59.044  | 0.000 | 1.361  | 1.361  |
| gotBu8_o t2 | 1.695  | 0.034 | 49.493  | 0.000 | 1.695  | 1.695  |
| gotBu8_o t3 | 1.889  | 0.045 | 42.038  | 0.000 | 1.889  | 1.889  |
| gotBu8_o t4 | 2.083  | 0.056 | 37.469  | 0.000 | 2.083  | 2.083  |
| gotBu9_o t1 | 1.492  | 0.032 | 46.509  | 0.000 | 1.492  | 1.492  |
| gotBu9_o t2 | 1.744  | 0.041 | 42.727  | 0.000 | 1.744  | 1.744  |
| gotBu9_o t3 | 1.889  | 0.044 | 43.041  | 0.000 | 1.889  | 1.889  |
| gotBu9_o t4 | 2.075  | 0.047 | 44.068  | 0.000 | 2.075  | 2.075  |
| depre1_o t1 | -0.553 | 0.024 | -22.682 | 0.000 | -0.553 | -0.553 |
| depre1_o t2 | 0.163  | 0.023 | 7.209   | 0.000 | 0.163  | 0.163  |
| depre1_o t3 | 1.095  | 0.030 | 36.002  | 0.000 | 1.095  | 1.095  |

# An indirect effect model with ordinal data ...

|             |        |       |         |       |        |        |
|-------------|--------|-------|---------|-------|--------|--------|
| depre1_o t4 | 1.812  | 0.045 | 40.615  | 0.000 | 1.812  | 1.812  |
| depre2_o t1 | -0.906 | 0.016 | -56.190 | 0.000 | -0.906 | -0.906 |
| depre2_o t2 | -0.175 | 0.021 | -8.350  | 0.000 | -0.175 | -0.175 |
| depre2_o t3 | 0.749  | 0.022 | 34.483  | 0.000 | 0.749  | 0.749  |
| depre2_o t4 | 1.533  | 0.043 | 35.647  | 0.000 | 1.533  | 1.533  |
| depre3_o t1 | 0.293  | 0.027 | 10.846  | 0.000 | 0.293  | 0.293  |
| depre3_o t2 | 0.687  | 0.028 | 24.871  | 0.000 | 0.687  | 0.687  |
| depre3_o t3 | 1.168  | 0.033 | 35.902  | 0.000 | 1.168  | 1.168  |
| depre3_o t4 | 1.642  | 0.045 | 36.773  | 0.000 | 1.642  | 1.642  |
| depre4_o t1 | -0.152 | 0.019 | -8.014  | 0.000 | -0.152 | -0.152 |
| depre4_o t2 | 0.247  | 0.022 | 11.418  | 0.000 | 0.247  | 0.247  |
| depre4_o t3 | 0.897  | 0.023 | 38.568  | 0.000 | 0.897  | 0.897  |
| depre4_o t4 | 1.478  | 0.034 | 44.095  | 0.000 | 1.478  | 1.478  |
| depre5_o t1 | -0.410 | 0.027 | -15.402 | 0.000 | -0.410 | -0.410 |
| depre5_o t2 | 0.053  | 0.023 | 2.309   | 0.021 | 0.053  | 0.053  |
| depre5_o t3 | 0.656  | 0.029 | 22.299  | 0.000 | 0.656  | 0.656  |
| depre5_o t4 | 1.237  | 0.034 | 36.805  | 0.000 | 1.237  | 1.237  |
| depre6_o t1 | -0.454 | 0.026 | -17.201 | 0.000 | -0.454 | -0.454 |
| depre6_o t2 | 0.092  | 0.021 | 4.326   | 0.000 | 0.092  | 0.092  |
| depre6_o t3 | 0.733  | 0.013 | 55.029  | 0.000 | 0.733  | 0.733  |
| depre6_o t4 | 1.261  | 0.025 | 49.514  | 0.000 | 1.261  | 1.261  |
| alc1_o t1   | 1.060  | 0.040 | 26.290  | 0.000 | 1.060  | 1.060  |
| alc1_o t2   | 1.836  | 0.044 | 41.357  | 0.000 | 1.836  | 1.836  |
| alc1_o t3   | 2.193  | 0.053 | 41.417  | 0.000 | 2.193  | 2.193  |
| alc1_o t4   | 2.435  | 0.090 | 27.033  | 0.000 | 2.435  | 2.435  |
| alc2_o t1   | 0.927  | 0.030 | 30.765  | 0.000 | 0.927  | 0.927  |

## An indirect effect model with ordinal data ...

|                   |                 |                |                |                   |               |                |
|-------------------|-----------------|----------------|----------------|-------------------|---------------|----------------|
| alc2_o t2         | 1.816           | 0.051          | 35.610         | 0.000             | 1.816         | 1.816          |
| alc2_o t3         | 2.117           | 0.053          | 40.178         | 0.000             | 2.117         | 2.117          |
| alc2_o t4         | 2.473           | 0.079          | 31.118         | 0.000             | 2.473         | 2.473          |
| alc3_o t1         | 1.317           | 0.029          | 45.335         | 0.000             | 1.317         | 1.317          |
| alc3_o t2         | 1.816           | 0.036          | 49.846         | 0.000             | 1.816         | 1.816          |
| alc3_o t3         | 2.075           | 0.050          | 41.333         | 0.000             | 2.075         | 2.075          |
| alc3_o t4         | 2.435           | 0.103          | 23.677         | 0.000             | 2.435         | 2.435          |
| alc4_o t1         | 0.983           | 0.024          | 40.889         | 0.000             | 0.983         | 0.983          |
| alc4_o t2         | 1.604           | 0.038          | 42.494         | 0.000             | 1.604         | 1.604          |
| alc4_o t3         | 2.000           | 0.029          | 68.147         | 0.000             | 2.000         | 2.000          |
| alc4_o t4         | 2.353           | 0.060          | 39.476         | 0.000             | 2.353         | 2.353          |
| alc5_o t1         | 1.067           | 0.027          | 39.306         | 0.000             | 1.067         | 1.067          |
| alc5_o t2         | 1.719           | 0.030          | 56.984         | 0.000             | 1.719         | 1.719          |
| alc5_o t3         | 2.036           | 0.041          | 49.952         | 0.000             | 2.036         | 2.036          |
| alc5_o t4         | 2.353           | 0.079          | 29.659         | 0.000             | 2.353         | 2.353          |
| <b>Variances:</b> |                 |                |                |                   |               |                |
|                   | <b>Estimate</b> | <b>Std.Err</b> | <b>z-value</b> | <b>P(&gt; z )</b> | <b>Std.lv</b> | <b>Std.all</b> |
| gotBully          | 1.000           |                |                |                   | 1.000         | 1.000          |
| .depress          | 1.000           |                |                |                   | 0.808         | 0.808          |
| .alcohol          | 1.000           |                |                |                   | 0.861         | 0.861          |
| .gotBu1_o         | 0.435           |                |                |                   | 0.435         | 0.435          |
| .gotBu2_o         | 0.391           |                |                |                   | 0.391         | 0.391          |
| .gotBu3_o         | 0.395           |                |                |                   | 0.395         | 0.395          |
| .gotBu4_o         | 0.348           |                |                |                   | 0.348         | 0.348          |
| .gotBu5_o         | 0.295           |                |                |                   | 0.295         | 0.295          |

# An indirect effect model with ordinal data ...

|            |          |         |         |         |        |         |
|------------|----------|---------|---------|---------|--------|---------|
| .gotBu6_o  | 0.249    |         |         |         | 0.249  | 0.249   |
| .gotBu7_o  | 0.407    |         |         |         | 0.407  | 0.407   |
| .gotBu8_o  | 0.259    |         |         |         | 0.259  | 0.259   |
| .gotBu9_o  | 0.206    |         |         |         | 0.206  | 0.206   |
| .depre1_o  | 0.521    |         |         |         | 0.521  | 0.521   |
| .depre2_o  | 0.591    |         |         |         | 0.591  | 0.591   |
| .depre3_o  | 0.432    |         |         |         | 0.432  | 0.432   |
| .depre4_o  | 0.495    |         |         |         | 0.495  | 0.495   |
| .depre5_o  | 0.643    |         |         |         | 0.643  | 0.643   |
| .depre6_o  | 0.606    |         |         |         | 0.606  | 0.606   |
| .alc1_o    | 0.262    |         |         |         | 0.262  | 0.262   |
| .alc2_o    | 0.401    |         |         |         | 0.401  | 0.401   |
| .alc3_o    | 0.095    |         |         |         | 0.095  | 0.095   |
| .alc4_o    | 0.221    |         |         |         | 0.221  | 0.221   |
| .alc5_o    | 0.178    |         |         |         | 0.178  | 0.178   |
| Scales y*: |          |         |         |         |        |         |
|            | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| gotBu1_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu2_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu3_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu4_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu5_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu6_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu7_o   | 1.000    |         |         |         | 1.000  | 1.000   |
| gotBu8_o   | 1.000    |         |         |         | 1.000  | 1.000   |

# An indirect effect model with ordinal data ...

|          |       |  |  |  |       |       |
|----------|-------|--|--|--|-------|-------|
| gotBu9_o | 1.000 |  |  |  | 1.000 | 1.000 |
| depre1_o | 1.000 |  |  |  | 1.000 | 1.000 |
| depre2_o | 1.000 |  |  |  | 1.000 | 1.000 |
| depre3_o | 1.000 |  |  |  | 1.000 | 1.000 |
| depre4_o | 1.000 |  |  |  | 1.000 | 1.000 |
| depre5_o | 1.000 |  |  |  | 1.000 | 1.000 |
| depre6_o | 1.000 |  |  |  | 1.000 | 1.000 |
| alc1_o   | 1.000 |  |  |  | 1.000 | 1.000 |
| alc2_o   | 1.000 |  |  |  | 1.000 | 1.000 |
| alc3_o   | 1.000 |  |  |  | 1.000 | 1.000 |
| alc4_o   | 1.000 |  |  |  | 1.000 | 1.000 |
| alc5_o   | 1.000 |  |  |  | 1.000 | 1.000 |

## Defined Parameters:

|       | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-------|----------|---------|---------|---------|--------|---------|
| ab    | 0.140    | 0.026   | 5.295   | 0.000   | 0.129  | 0.129   |
| total | 0.283    | 0.037   | 7.652   | 0.000   | 0.262  | 0.262   |

# Outline

- 1 Two Meanings of Non-Normality
- 2 Should Ordinal Data Be Treated as Numeric Data?
  - Current common practices
  - Ordinal data should be modeled differently
  - Ordinal data can be treated as numeric (with caution!)
- 3 Estimators for categorical data
- 4 CFA Models with Ordinal Data
  - Data input/type
  - CFA Models with Ordinal Data from HBSC
- 5 Structural Models with Ordinal Data
  - Direct regressive models
  - Indirect effect (mediation) models
- 6 Measurement Invariance Testing with Ordinal Data

# Measurement invariance testing - configural invariance

```
## Specifying the model-structure object
model.config.WLSMV <- '
  depress =~ depre1_o + depre2_o + depre3_o +
             depre4_o + depre5_o + depre6_o '
## Estimating the model
fit.config.WLSMV <-
  cfa(model = model.config.WLSMV, data = hbsc,
      mimic = "Mplus", estimator = "WLSMV",
      std.lv = TRUE, group = "Grade",
      ordered = c("depre1_o", "depre2_o",
                  "depre3_o",
                  "depre4_o", "depre5_o",
                  "depre6_o"))
## Requesting an estimation summary
summary(fit.config.WLSMV, fit.measures = TRUE,
        standardized = TRUE)
```

# Measurement invariance testing - configural invariance ...

```

lavaan 0.6-3 ended normally after 10 iterations

Optimization method                NLMINB
Number of free parameters           60

Number of observations per group
7                                   1811      1880
6                                   2292      2404

Estimator                           DWLS      Robust
Model Fit Test Statistic            180.000   333.412
Degrees of freedom                   18       18
P-value (Chi-square)                0.000    0.000
Scaling correction factor            0.541
Shift parameter for each group:
7                                   0.240
6                                   0.304
  for simple second-order correction (WLSMV)

Chi-square for each group:
7                                   68.577   127.057
6                                   111.423  206.355

```



# Measurement invariance testing - configural invariance ...

Model test baseline model:

|                                 |           |           |
|---------------------------------|-----------|-----------|
| Minimum Function Test Statistic | 16164.928 | 11074.106 |
| Degrees of freedom              | 30        | 30        |
| P-value                         | 0.000     | 0.000     |

User model versus baseline model:

|                                    |       |       |
|------------------------------------|-------|-------|
| Comparative Fit Index (CFI)        | 0.990 | 0.971 |
| Tucker-Lewis Index (TLI)           | 0.983 | 0.952 |
| Robust Comparative Fit Index (CFI) |       | NA    |
| Robust Tucker-Lewis Index (TLI)    |       | NA    |

Root Mean Square Error of Approximation:

|                                |             |       |
|--------------------------------|-------------|-------|
| RMSEA                          | 0.066       | 0.092 |
| 90 Percent Confidence Interval | 0.058 0.075 | 0.084 |
| 0.101                          |             |       |
| P-value RMSEA <= 0.05          | 0.001       | 0.000 |
| Robust RMSEA                   |             | NA    |
| 90 Percent Confidence Interval |             | NA    |
| NA                             |             |       |

Standardized Root Mean Square Residual:

# Measurement invariance testing - configural invariance ...

|                                     |          |         |         |         |              |         |
|-------------------------------------|----------|---------|---------|---------|--------------|---------|
| SRMR                                |          |         | 0.035   |         | 0.035        |         |
| Weighted Root Mean Square Residual: |          |         |         |         |              |         |
| WRMR                                |          |         | 2.148   |         | 2.148        |         |
| Parameter Estimates:                |          |         |         |         |              |         |
| Information                         |          |         |         |         | Expected     |         |
| Information saturated (h1) model    |          |         |         |         | Unstructured |         |
| Standard Errors                     |          |         |         |         | Robust.sem   |         |
| Group 1 [7]:                        |          |         |         |         |              |         |
| Latent Variables:                   |          |         |         |         |              |         |
|                                     | Estimate | Std.Err | z-value | P(> z ) | Std.lv       | Std.all |
| depress =~                          |          |         |         |         |              |         |
| depre1_o                            | 0.704    | 0.016   | 45.352  | 0.000   | 0.704        | 0.704   |
| depre2_o                            | 0.649    | 0.016   | 39.702  | 0.000   | 0.649        | 0.649   |
| depre3_o                            | 0.749    | 0.017   | 44.639  | 0.000   | 0.749        | 0.749   |
| depre4_o                            | 0.733    | 0.016   | 46.213  | 0.000   | 0.733        | 0.733   |
| depre5_o                            | 0.600    | 0.019   | 31.717  | 0.000   | 0.600        | 0.600   |
| depre6_o                            | 0.619    | 0.018   | 34.057  | 0.000   | 0.619        | 0.619   |

## Measurement invariance testing - configural invariance ...

| Intercepts: |          |         |         |         |        |         |
|-------------|----------|---------|---------|---------|--------|---------|
|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| .depre1_o   | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre2_o   | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre3_o   | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre4_o   | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre5_o   | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre6_o   | 0.000    |         |         |         | 0.000  | 0.000   |
| depress     | 0.000    |         |         |         | 0.000  | 0.000   |
| Thresholds: |          |         |         |         |        |         |
|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depre1_o t1 | -0.591   | 0.031   | -18.818 | 0.000   | -0.591 | -0.591  |
| depre1_o t2 | 0.142    | 0.030   | 4.813   | 0.000   | 0.142  | 0.142   |
| depre1_o t3 | 1.089    | 0.037   | 29.607  | 0.000   | 1.089  | 1.089   |
| depre1_o t4 | 1.780    | 0.055   | 32.594  | 0.000   | 1.780  | 1.780   |
| depre2_o t1 | -0.945   | 0.035   | -27.171 | 0.000   | -0.945 | -0.945  |
| depre2_o t2 | -0.214   | 0.030   | -7.205  | 0.000   | -0.214 | -0.214  |
| depre2_o t3 | 0.747    | 0.033   | 22.876  | 0.000   | 0.747  | 0.747   |
| depre2_o t4 | 1.535    | 0.046   | 33.153  | 0.000   | 1.535  | 1.535   |
| depre3_o t1 | 0.294    | 0.030   | 9.827   | 0.000   | 0.294  | 0.294   |
| depre3_o t2 | 0.702    | 0.032   | 21.762  | 0.000   | 0.702  | 0.702   |
| depre3_o t3 | 1.210    | 0.039   | 31.169  | 0.000   | 1.210  | 1.210   |
| depre3_o t4 | 1.722    | 0.052   | 32.872  | 0.000   | 1.722  | 1.722   |
| depre4_o t1 | -0.094   | 0.030   | -3.170  | 0.002   | -0.094 | -0.094  |
| depre4_o t2 | 0.267    | 0.030   | 8.938   | 0.000   | 0.267  | 0.267   |

## Measurement invariance testing - configural invariance ...

|             |        |       |         |       |        |        |
|-------------|--------|-------|---------|-------|--------|--------|
| depre4_o t3 | 0.907  | 0.034 | 26.424  | 0.000 | 0.907  | 0.907  |
| depre4_o t4 | 1.504  | 0.045 | 33.104  | 0.000 | 1.504  | 1.504  |
| depre5_o t1 | -0.394 | 0.030 | -13.000 | 0.000 | -0.394 | -0.394 |
| depre5_o t2 | 0.070  | 0.029 | 2.372   | 0.018 | 0.070  | 0.070  |
| depre5_o t3 | 0.697  | 0.032 | 21.627  | 0.000 | 0.697  | 0.697  |
| depre5_o t4 | 1.279  | 0.040 | 31.862  | 0.000 | 1.279  | 1.279  |
| depre6_o t1 | -0.481 | 0.031 | -15.645 | 0.000 | -0.481 | -0.481 |
| depre6_o t2 | 0.069  | 0.029 | 2.325   | 0.020 | 0.069  | 0.069  |
| depre6_o t3 | 0.727  | 0.032 | 22.387  | 0.000 | 0.727  | 0.727  |
| depre6_o t4 | 1.230  | 0.039 | 31.389  | 0.000 | 1.230  | 1.230  |

## Variances :

|           | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-----------|----------|---------|---------|---------|--------|---------|
| .depre1_o | 0.504    |         |         |         | 0.504  | 0.504   |
| .depre2_o | 0.578    |         |         |         | 0.578  | 0.578   |
| .depre3_o | 0.438    |         |         |         | 0.438  | 0.438   |
| .depre4_o | 0.463    |         |         |         | 0.463  | 0.463   |
| .depre5_o | 0.640    |         |         |         | 0.640  | 0.640   |
| .depre6_o | 0.617    |         |         |         | 0.617  | 0.617   |
| depress   | 1.000    |         |         |         | 1.000  | 1.000   |

## Scales y\*:

|          | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|----------|---------|---------|---------|--------|---------|
| depre1_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre2_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre3_o | 1.000    |         |         |         | 1.000  | 1.000   |

## Measurement invariance testing - configural invariance ...

|          |       |  |  |       |       |
|----------|-------|--|--|-------|-------|
| depre4_o | 1.000 |  |  | 1.000 | 1.000 |
| depre5_o | 1.000 |  |  | 1.000 | 1.000 |
| depre6_o | 1.000 |  |  | 1.000 | 1.000 |

Group 2 [6]:

Latent Variables:

|            | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|------------|----------|---------|---------|---------|--------|---------|
| depress =~ |          |         |         |         |        |         |
| depre1_o   | 0.716    | 0.013   | 53.121  | 0.000   | 0.716  | 0.716   |
| depre2_o   | 0.659    | 0.015   | 44.443  | 0.000   | 0.659  | 0.659   |
| depre3_o   | 0.745    | 0.015   | 49.442  | 0.000   | 0.745  | 0.745   |
| depre4_o   | 0.701    | 0.015   | 47.571  | 0.000   | 0.701  | 0.701   |
| depre5_o   | 0.604    | 0.017   | 35.803  | 0.000   | 0.604  | 0.604   |
| depre6_o   | 0.566    | 0.018   | 31.571  | 0.000   | 0.566  | 0.566   |

Intercepts:

|           | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-----------|----------|---------|---------|---------|--------|---------|
| .depre1_o | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre2_o | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre3_o | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre4_o | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre5_o | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre6_o | 0.000    |         |         |         | 0.000  | 0.000   |
| depress   | 0.000    |         |         |         | 0.000  | 0.000   |

## Measurement invariance testing - configural invariance ...

55 Thresholds :

|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-------------|----------|---------|---------|---------|--------|---------|
| depre1_o t1 | -0.543   | 0.028   | -19.637 | 0.000   | -0.543 | -0.543  |
| depre1_o t2 | 0.125    | 0.026   | 4.759   | 0.000   | 0.125  | 0.125   |
| depre1_o t3 | 1.100    | 0.033   | 33.486  | 0.000   | 1.100  | 1.100   |
| depre1_o t4 | 1.791    | 0.049   | 36.599  | 0.000   | 1.791  | 1.791   |
| depre2_o t1 | -0.815   | 0.030   | -27.511 | 0.000   | -0.815 | -0.815  |
| depre2_o t2 | -0.177   | 0.026   | -6.719  | 0.000   | -0.177 | -0.177  |
| depre2_o t3 | 0.729    | 0.029   | 25.240  | 0.000   | 0.729  | 0.729   |
| depre2_o t4 | 1.490    | 0.040   | 37.208  | 0.000   | 1.490  | 1.490   |
| depre3_o t1 | 0.285    | 0.027   | 10.717  | 0.000   | 0.285  | 0.285   |
| depre3_o t2 | 0.642    | 0.028   | 22.722  | 0.000   | 0.642  | 0.642   |
| depre3_o t3 | 1.151    | 0.034   | 34.279  | 0.000   | 1.151  | 1.151   |
| depre3_o t4 | 1.557    | 0.042   | 37.320  | 0.000   | 1.557  | 1.557   |
| depre4_o t1 | -0.117   | 0.026   | -4.467  | 0.000   | -0.117 | -0.117  |
| depre4_o t2 | 0.246    | 0.026   | 9.303   | 0.000   | 0.246  | 0.246   |
| depre4_o t3 | 0.874    | 0.030   | 28.964  | 0.000   | 0.874  | 0.874   |
| depre4_o t4 | 1.386    | 0.038   | 36.729  | 0.000   | 1.386  | 1.386   |
| depre5_o t1 | -0.350   | 0.027   | -13.084 | 0.000   | -0.350 | -0.350  |
| depre5_o t2 | 0.073    | 0.026   | 2.797   | 0.005   | 0.073  | 0.073   |
| depre5_o t3 | 0.647    | 0.028   | 22.883  | 0.000   | 0.647  | 0.647   |
| depre5_o t4 | 1.197    | 0.034   | 34.907  | 0.000   | 1.197  | 1.197   |
| depre6_o t1 | -0.388   | 0.027   | -14.410 | 0.000   | -0.388 | -0.388  |
| depre6_o t2 | 0.097    | 0.026   | 3.716   | 0.000   | 0.097  | 0.097   |
| depre6_o t3 | 0.752    | 0.029   | 25.872  | 0.000   | 0.752  | 0.752   |

## Measurement invariance testing - configural invariance ...

|             |          |         |         |         |        |         |
|-------------|----------|---------|---------|---------|--------|---------|
| depre6_o t4 | 1.275    | 0.036   | 35.805  | 0.000   | 1.275  | 1.275   |
| Variances:  |          |         |         |         |        |         |
|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| .depre1_o   | 0.487    |         |         |         | 0.487  | 0.487   |
| .depre2_o   | 0.565    |         |         |         | 0.565  | 0.565   |
| .depre3_o   | 0.446    |         |         |         | 0.446  | 0.446   |
| .depre4_o   | 0.509    |         |         |         | 0.509  | 0.509   |
| .depre5_o   | 0.635    |         |         |         | 0.635  | 0.635   |
| .depre6_o   | 0.680    |         |         |         | 0.680  | 0.680   |
| depress     | 1.000    |         |         |         | 1.000  | 1.000   |
| Scales y*:  |          |         |         |         |        |         |
|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depre1_o    | 1.000    |         |         |         | 1.000  | 1.000   |
| depre2_o    | 1.000    |         |         |         | 1.000  | 1.000   |
| depre3_o    | 1.000    |         |         |         | 1.000  | 1.000   |
| depre4_o    | 1.000    |         |         |         | 1.000  | 1.000   |
| depre5_o    | 1.000    |         |         |         | 1.000  | 1.000   |
| depre6_o    | 1.000    |         |         |         | 1.000  | 1.000   |

# Measurement invariance testing - metric/weak invariance

```
## Specifying the model-structure object
model.metric.WLSMV <- '
  depress =~ depre1_o + depre2_o + depre3_o +
             depre4_o + depre5_o + depre6_o
  depress ~ c(1, NA)*depress '
## Estimating the model
fit.metric.WLSMV <-
  cfa(model = model.metric.WLSMV, data = hbsc,
      mimic = "Mplus", estimator = "WLSMV",
      std.lv = TRUE, group = "Grade",
      ordered = c("depre1_o", "depre2_o",
                  "depre3_o", "depre4_o", "depre5_o",
                  "depre6_o"),
      group.equal = "loadings")
## Requesting an estimation summary
summary(fit.metric.WLSMV, fit.measures = TRUE,
        standardized = TRUE)
```



# Measurement invariance testing - metric/weak invariance

...

```
lavaan 0.6-3 ended normally after 11 iterations

  Optimization method          NLMINB
  Number of free parameters      61
  Number of equality constraints   6

                                     Used      Total
  Number of observations per group
  7                               1811      1880
  6                               2292      2404

  Estimator          DWLS          Robust
  Model Fit Test Statistic  188.866    306.223
  Degrees of freedom        23          23
  P-value (Chi-square)      0.000        0.000
  Scaling correction factor              0.614
  Shift parameter for each group:
  7                               -0.654
  6                               -0.827
  for simple second-order correction (WLSMV)

Chi-square for each group:
```

# Measurement invariance testing - metric/weak invariance

...

|  |             |           |
|--|-------------|-----------|
| 7  | 73.253      | 118.692   |
| 6  | 115.613     | 187.532   |
| Model test baseline model:               |             |           |
| Minimum Function Test Statistic          | 16164.928   | 11074.106 |
| Degrees of freedom                       | 30          | 30        |
| P-value                                  | 0.000       | 0.000     |
| User model versus baseline model:        |             |           |
| Comparative Fit Index (CFI)              | 0.990       | 0.974     |
| Tucker-Lewis Index (TLI)                 | 0.987       | 0.967     |
| Robust Comparative Fit Index (CFI)       |             | NA        |
| Robust Tucker-Lewis Index (TLI)          |             | NA        |
| Root Mean Square Error of Approximation: |             |           |
| RMSEA                                    | 0.059       | 0.077     |
| 90 Percent Confidence Interval           | 0.052 0.067 | 0.070     |
| 0.085                                    |             |           |
| P-value RMSEA <= 0.05                    | 0.024       | 0.000     |

# Measurement invariance testing - metric/weak invariance

...

```

Robust RMSEA
90 Percent Confidence Interval
    NA
    NA

Standardized Root Mean Square Residual:

    SRMR                                0.036      0.036

Weighted Root Mean Square Residual:

    WRMR                                2.201      2.201

Parameter Estimates:

    Information                          Expected
    Information saturated (h1) model      Unstructured
    Standard Errors                       Robust.sem

Group 1 [7]:

Latent Variables:
    Estimate   Std.Err   z-value   P(>|z|)   Std.lv   Std.all
depress =~

```

# Measurement invariance testing - metric/weak invariance

...

|                    |          |         |         |         |        |         |
|--------------------|----------|---------|---------|---------|--------|---------|
| depre1_ (.p1.)     | 0.716    | 0.012   | 57.884  | 0.000   | 0.716  | 0.716   |
| depre2_ (.p2.)     | 0.660    | 0.013   | 52.740  | 0.000   | 0.660  | 0.660   |
| depre3_ (.p3.)     | 0.753    | 0.013   | 56.179  | 0.000   | 0.753  | 0.753   |
| depre4_ (.p4.)     | 0.721    | 0.013   | 57.062  | 0.000   | 0.721  | 0.721   |
| depre5_ (.p5.)     | 0.607    | 0.014   | 43.681  | 0.000   | 0.607  | 0.607   |
| depre6_ (.p6.)     | 0.595    | 0.014   | 42.722  | 0.000   | 0.595  | 0.595   |
| <b>Intercepts:</b> |          |         |         |         |        |         |
|                    | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| .depre1_o          | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre2_o          | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre3_o          | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre4_o          | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre5_o          | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre6_o          | 0.000    |         |         |         | 0.000  | 0.000   |
| depress            | 0.000    |         |         |         | 0.000  | 0.000   |
| <b>Thresholds:</b> |          |         |         |         |        |         |
|                    | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depre1_o t1        | -0.591   | 0.031   | -18.818 | 0.000   | -0.591 | -0.591  |
| depre1_o t2        | 0.142    | 0.030   | 4.813   | 0.000   | 0.142  | 0.142   |
| depre1_o t3        | 1.089    | 0.037   | 29.607  | 0.000   | 1.089  | 1.089   |
| depre1_o t4        | 1.780    | 0.055   | 32.594  | 0.000   | 1.780  | 1.780   |
| depre2_o t1        | -0.945   | 0.035   | -27.171 | 0.000   | -0.945 | -0.945  |

# Measurement invariance testing - metric/weak invariance

...

|             |          |         |         |         |        |         |
|-------------|----------|---------|---------|---------|--------|---------|
| depre2_o t2 | -0.214   | 0.030   | -7.205  | 0.000   | -0.214 | -0.214  |
| depre2_o t3 | 0.747    | 0.033   | 22.876  | 0.000   | 0.747  | 0.747   |
| depre2_o t4 | 1.535    | 0.046   | 33.153  | 0.000   | 1.535  | 1.535   |
| depre3_o t1 | 0.294    | 0.030   | 9.827   | 0.000   | 0.294  | 0.294   |
| depre3_o t2 | 0.702    | 0.032   | 21.762  | 0.000   | 0.702  | 0.702   |
| depre3_o t3 | 1.210    | 0.039   | 31.169  | 0.000   | 1.210  | 1.210   |
| depre3_o t4 | 1.722    | 0.052   | 32.872  | 0.000   | 1.722  | 1.722   |
| depre4_o t1 | -0.094   | 0.030   | -3.170  | 0.002   | -0.094 | -0.094  |
| depre4_o t2 | 0.267    | 0.030   | 8.938   | 0.000   | 0.267  | 0.267   |
| depre4_o t3 | 0.907    | 0.034   | 26.424  | 0.000   | 0.907  | 0.907   |
| depre4_o t4 | 1.504    | 0.045   | 33.104  | 0.000   | 1.504  | 1.504   |
| depre5_o t1 | -0.394   | 0.030   | -13.000 | 0.000   | -0.394 | -0.394  |
| depre5_o t2 | 0.070    | 0.029   | 2.372   | 0.018   | 0.070  | 0.070   |
| depre5_o t3 | 0.697    | 0.032   | 21.627  | 0.000   | 0.697  | 0.697   |
| depre5_o t4 | 1.279    | 0.040   | 31.862  | 0.000   | 1.279  | 1.279   |
| depre6_o t1 | -0.481   | 0.031   | -15.645 | 0.000   | -0.481 | -0.481  |
| depre6_o t2 | 0.069    | 0.029   | 2.325   | 0.020   | 0.069  | 0.069   |
| depre6_o t3 | 0.727    | 0.032   | 22.387  | 0.000   | 0.727  | 0.727   |
| depre6_o t4 | 1.230    | 0.039   | 31.389  | 0.000   | 1.230  | 1.230   |
| Variances:  |          |         |         |         |        |         |
|             | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depress     | 1.000    |         |         |         | 1.000  | 1.000   |
| .depre1_o   | 0.487    |         |         |         | 0.487  | 0.487   |

# Measurement invariance testing - metric/weak invariance

...

|           |       |  |  |  |       |       |
|-----------|-------|--|--|--|-------|-------|
| .depre2_o | 0.565 |  |  |  | 0.565 | 0.565 |
| .depre3_o | 0.434 |  |  |  | 0.434 | 0.434 |
| .depre4_o | 0.480 |  |  |  | 0.480 | 0.480 |
| .depre5_o | 0.632 |  |  |  | 0.632 | 0.632 |
| .depre6_o | 0.646 |  |  |  | 0.646 | 0.646 |

## Scales y\*:

|          | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|----------|---------|---------|---------|--------|---------|
| depre1_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre2_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre3_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre4_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre5_o | 1.000    |         |         |         | 1.000  | 1.000   |
| depre6_o | 1.000    |         |         |         | 1.000  | 1.000   |

## Group 2 [6]:

## Latent Variables:

|                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------------|----------|---------|---------|---------|--------|---------|
| depress =~     |          |         |         |         |        |         |
| depre1_ (.p1.) | 0.716    | 0.012   | 57.884  | 0.000   | 0.706  | 0.706   |
| depre2_ (.p2.) | 0.660    | 0.013   | 52.740  | 0.000   | 0.650  | 0.650   |
| depre3_ (.p3.) | 0.753    | 0.013   | 56.179  | 0.000   | 0.742  | 0.742   |

# Measurement invariance testing - metric/weak invariance

...

|                |          |         |         |         |        |         |
|----------------|----------|---------|---------|---------|--------|---------|
| depre4_ (.p4.) | 0.721    | 0.013   | 57.062  | 0.000   | 0.711  | 0.711   |
| depre5_ (.p5.) | 0.607    | 0.014   | 43.681  | 0.000   | 0.598  | 0.598   |
| depre6_ (.p6.) | 0.595    | 0.014   | 42.722  | 0.000   | 0.587  | 0.587   |
| Intercepts:    |          |         |         |         |        |         |
|                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| .depre1_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre2_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre3_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre4_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre5_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre6_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| depress        | 0.000    |         |         |         | 0.000  | 0.000   |
| Thresholds:    |          |         |         |         |        |         |
|                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depre1_o t1    | -0.543   | 0.028   | -19.637 | 0.000   | -0.543 | -0.543  |
| depre1_o t2    | 0.125    | 0.026   | 4.759   | 0.000   | 0.125  | 0.125   |
| depre1_o t3    | 1.100    | 0.033   | 33.486  | 0.000   | 1.100  | 1.100   |
| depre1_o t4    | 1.791    | 0.049   | 36.599  | 0.000   | 1.791  | 1.791   |
| depre2_o t1    | -0.815   | 0.030   | -27.511 | 0.000   | -0.815 | -0.815  |
| depre2_o t2    | -0.177   | 0.026   | -6.719  | 0.000   | -0.177 | -0.177  |
| depre2_o t3    | 0.729    | 0.029   | 25.240  | 0.000   | 0.729  | 0.729   |
| depre2_o t4    | 1.490    | 0.040   | 37.208  | 0.000   | 1.490  | 1.490   |

# Measurement invariance testing - metric/weak invariance

...

|             |        |       |         |       |        |        |
|-------------|--------|-------|---------|-------|--------|--------|
| depre3_o t1 | 0.285  | 0.027 | 10.717  | 0.000 | 0.285  | 0.285  |
| depre3_o t2 | 0.642  | 0.028 | 22.722  | 0.000 | 0.642  | 0.642  |
| depre3_o t3 | 1.151  | 0.034 | 34.279  | 0.000 | 1.151  | 1.151  |
| depre3_o t4 | 1.557  | 0.042 | 37.320  | 0.000 | 1.557  | 1.557  |
| depre4_o t1 | -0.117 | 0.026 | -4.467  | 0.000 | -0.117 | -0.117 |
| depre4_o t2 | 0.246  | 0.026 | 9.303   | 0.000 | 0.246  | 0.246  |
| depre4_o t3 | 0.874  | 0.030 | 28.964  | 0.000 | 0.874  | 0.874  |
| depre4_o t4 | 1.386  | 0.038 | 36.729  | 0.000 | 1.386  | 1.386  |
| depre5_o t1 | -0.350 | 0.027 | -13.084 | 0.000 | -0.350 | -0.350 |
| depre5_o t2 | 0.073  | 0.026 | 2.797   | 0.005 | 0.073  | 0.073  |
| depre5_o t3 | 0.647  | 0.028 | 22.883  | 0.000 | 0.647  | 0.647  |
| depre5_o t4 | 1.197  | 0.034 | 34.907  | 0.000 | 1.197  | 1.197  |
| depre6_o t1 | -0.388 | 0.027 | -14.410 | 0.000 | -0.388 | -0.388 |
| depre6_o t2 | 0.097  | 0.026 | 3.716   | 0.000 | 0.097  | 0.097  |
| depre6_o t3 | 0.752  | 0.029 | 25.872  | 0.000 | 0.752  | 0.752  |
| depre6_o t4 | 1.275  | 0.036 | 35.805  | 0.000 | 1.275  | 1.275  |

## Variances:

|           | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-----------|----------|---------|---------|---------|--------|---------|
| depress   | 0.973    | 0.033   | 29.079  | 0.000   | 1.000  | 1.000   |
| .depre1_o | 0.501    |         |         |         | 0.501  | 0.501   |
| .depre2_o | 0.577    |         |         |         | 0.577  | 0.577   |
| .depre3_o | 0.449    |         |         |         | 0.449  | 0.449   |
| .depre4_o | 0.494    |         |         |         | 0.494  | 0.494   |



# Measurement invariance testing - metric/weak invariance

...

|            |           |          |         |         |         |                |
|------------|-----------|----------|---------|---------|---------|----------------|
| 90         | .depre5_o | 0.642    |         |         | 0.642   | 0.642          |
|            | .depre6_o | 0.655    |         |         | 0.655   | 0.655          |
| Scales y*: |           |          |         |         |         |                |
|            |           | Estimate | Std.Err | z-value | P(> z ) | Std.lv Std.all |
| 95         | depre1_o  | 1.000    |         |         |         | 1.000 1.000    |
|            | depre2_o  | 1.000    |         |         |         | 1.000 1.000    |
|            | depre3_o  | 1.000    |         |         |         | 1.000 1.000    |
|            | depre4_o  | 1.000    |         |         |         | 1.000 1.000    |
| 00         | depre5_o  | 1.000    |         |         |         | 1.000 1.000    |
|            | depre6_o  | 1.000    |         |         |         | 1.000 1.000    |

```

## Conducting a corrected chi-square test
## Comparing the configural and the metric model
lavTestLRT(fit.config.WLSMV, fit.metric.WLSMV,
           method = "satorra.bentler.2010",
           A.method = "delta")

```

# Measurement invariance testing - metric/weak invariance

...

```
Scaled Chi Square Difference Test (method = "satorra.bentler.2010")

          Df AIC BIC   Chisq Chisq diff Df diff Pr(>Chisq)
fit.config.WLSMV 18          180.00
fit.metric.WLSMV 23          188.87    10.124      5    0.0718 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

# Measurement invariance testing - scalar/strength invariance

```
## Specifying the model-structure object
model.scalar.WLSMV <- '
  depress =~ depre1_o + depre2_o + depre3_o +
            depre4_o + depre5_o + depre6_o
  depress ~ c(1, NA)*depress
  depress ~ c(0, NA)*1'
## Estimating the model
fit.scalar.WLSMV <-
  cfa(model = model.scalar.WLSMV, data = hbsc,
      mimic = "Mplus", estimator = "WLSMV",
      std.lv = TRUE, group = "Grade",
      ordered = c("depre1_o", "depre2_o",
                  "depre3_o", "depre4_o", "depre5_o",
                  "depre6_o"),
      group.equal = c("loadings", "thresholds"))
## Requesting an estimation summary
summary(fit.scalar.WLSMV, fit.measures = TRUE,
```

# Measurement invariance testing - scalar/stroing invariance

```
standardized = TRUE)
```

```
lavaan 0.6-3 ended normally after 27 iterations
```

```

Optimization method           NLMINB
Number of free parameters      68
Number of equality constraints  30

                                     Used      Total
Number of observations per group
7                                   1811     1880
6                                   2292     2404

Estimator           DWLS           Robust
Model Fit Test Statistic  201.376   330.890
Degrees of freedom        40        40
P-value (Chi-square)     0.000     0.000
Scaling correction factor           0.603
Shift parameter for each group:
7                                   -1.415
6                                   -1.791
for simple second-order correction (WLSMV)

```

# Measurement invariance testing - scalar/stroing invariance

...

Chi-square for each group:

|   |         |         |
|---|---------|---------|
| 7 | 79.770  | 130.929 |
| 6 | 121.605 | 199.960 |

Model test baseline model:

|                                 |           |           |
|---------------------------------|-----------|-----------|
| Minimum Function Test Statistic | 16164.928 | 11074.106 |
| Degrees of freedom              | 30        | 30        |
| P-value                         | 0.000     | 0.000     |

User model versus baseline model:

|                             |       |       |
|-----------------------------|-------|-------|
| Comparative Fit Index (CFI) | 0.990 | 0.974 |
| Tucker-Lewis Index (TLI)    | 0.992 | 0.980 |

|                                    |  |    |
|------------------------------------|--|----|
| Robust Comparative Fit Index (CFI) |  | NA |
| Robust Tucker-Lewis Index (TLI)    |  | NA |

Root Mean Square Error of Approximation:

|                                |             |       |
|--------------------------------|-------------|-------|
| RMSEA                          | 0.044       | 0.060 |
| 90 Percent Confidence Interval | 0.038 0.051 | 0.054 |
| 0.066                          |             |       |

# Measurement invariance testing - scalar/stroing invariance

...

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|                       |       |       |
|-----------------------|-------|-------|
| P-value RMSEA <= 0.05 | 0.933 | 0.004 |
|-----------------------|-------|-------|

|              |  |    |
|--------------|--|----|
| Robust RMSEA |  | NA |
|--------------|--|----|

|                                |  |    |
|--------------------------------|--|----|
| 90 Percent Confidence Interval |  | NA |
|--------------------------------|--|----|

|    |  |  |
|----|--|--|
| NA |  |  |
|----|--|--|

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Standardized Root Mean Square Residual:

|      |       |       |
|------|-------|-------|
| SRMR | 0.037 | 0.037 |
|------|-------|-------|

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Weighted Root Mean Square Residual:

|      |       |       |
|------|-------|-------|
| WRMR | 2.272 | 2.272 |
|------|-------|-------|

Parameter Estimates:

|             |  |          |
|-------------|--|----------|
| Information |  | Expected |
|-------------|--|----------|

|                                  |  |              |
|----------------------------------|--|--------------|
| Information saturated (h1) model |  | Unstructured |
|----------------------------------|--|--------------|

|                 |  |            |
|-----------------|--|------------|
| Standard Errors |  | Robust.sem |
|-----------------|--|------------|

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Group 1 [7]:

Latent Variables:

# Measurement invariance testing - scalar/stroing invariance

...

|                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------------|----------|---------|---------|---------|--------|---------|
| depress =~     |          |         |         |         |        |         |
| depre1_ (.p1.) | 0.701    | 0.013   | 52.266  | 0.000   | 0.701  | 0.701   |
| depre2_ (.p2.) | 0.656    | 0.014   | 47.410  | 0.000   | 0.656  | 0.656   |
| depre3_ (.p3.) | 0.760    | 0.015   | 51.150  | 0.000   | 0.760  | 0.760   |
| depre4_ (.p4.) | 0.732    | 0.014   | 52.459  | 0.000   | 0.732  | 0.732   |
| depre5_ (.p5.) | 0.607    | 0.016   | 38.229  | 0.000   | 0.607  | 0.607   |
| depre6_ (.p6.) | 0.598    | 0.015   | 38.668  | 0.000   | 0.598  | 0.598   |
| Intercepts:    |          |         |         |         |        |         |
|                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depress        | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre1_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre2_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre3_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre4_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre5_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| .depre6_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| Thresholds:    |          |         |         |         |        |         |
|                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| dpr1_ 1 (.p9.) | -0.585   | 0.027   | -21.689 | 0.000   | -0.585 | -0.585  |
| dpr1_ 2 (.10.) | 0.121    | 0.024   | 4.979   | 0.000   | 0.121  | 0.121   |
| dpr1_ 3 (.11.) | 1.096    | 0.032   | 34.556  | 0.000   | 1.096  | 1.096   |

# Measurement invariance testing - scalar/strong invariance

...

|                 |        |       |         |       |        |        |
|-----------------|--------|-------|---------|-------|--------|--------|
| dpr1_  4 (.12.) | 1.795  | 0.046 | 39.323  | 0.000 | 1.795  | 1.795  |
| dpr2_  1 (.13.) | -0.910 | 0.029 | -30.906 | 0.000 | -0.910 | -0.910 |
| dpr2_  2 (.14.) | -0.212 | 0.024 | -8.750  | 0.000 | -0.212 | -0.212 |
| dpr2_  3 (.15.) | 0.746  | 0.027 | 27.431  | 0.000 | 0.746  | 0.746  |
| dpr2_  4 (.16.) | 1.542  | 0.039 | 39.662  | 0.000 | 1.542  | 1.542  |
| dpr3_  1 (.17.) | 0.288  | 0.025 | 11.339  | 0.000 | 0.288  | 0.288  |
| dpr3_  2 (.18.) | 0.685  | 0.028 | 24.794  | 0.000 | 0.685  | 0.685  |
| dpr3_  3 (.19.) | 1.216  | 0.034 | 35.475  | 0.000 | 1.216  | 1.216  |
| dpr3_  4 (.20.) | 1.687  | 0.044 | 38.010  | 0.000 | 1.687  | 1.687  |
| dpr4_  1 (.21.) | -0.125 | 0.025 | -4.968  | 0.000 | -0.125 | -0.125 |
| dpr4_  2 (.22.) | 0.255  | 0.025 | 10.072  | 0.000 | 0.255  | 0.255  |
| dpr4_  3 (.23.) | 0.919  | 0.030 | 30.898  | 0.000 | 0.919  | 0.919  |
| dpr4_  4 (.24.) | 1.496  | 0.039 | 38.146  | 0.000 | 1.496  | 1.496  |
| dpr5_  1 (.25.) | -0.395 | 0.025 | -15.905 | 0.000 | -0.395 | -0.395 |
| dpr5_  2 (.26.) | 0.063  | 0.023 | 2.678   | 0.007 | 0.063  | 0.063  |
| dpr5_  3 (.27.) | 0.682  | 0.027 | 25.599  | 0.000 | 0.682  | 0.682  |
| dpr5_  4 (.28.) | 1.265  | 0.035 | 36.570  | 0.000 | 1.265  | 1.265  |
| dpr6_  1 (.29.) | -0.458 | 0.025 | -18.069 | 0.000 | -0.458 | -0.458 |
| dpr6_  2 (.30.) | 0.076  | 0.024 | 3.238   | 0.001 | 0.076  | 0.076  |
| dpr6_  3 (.31.) | 0.757  | 0.027 | 27.625  | 0.000 | 0.757  | 0.757  |
| dpr6_  4 (.32.) | 1.289  | 0.034 | 37.377  | 0.000 | 1.289  | 1.289  |

Variances:

| Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|---------|---------|---------|--------|---------|
|----------|---------|---------|---------|--------|---------|



# Measurement invariance testing - scalar/stroing invariance

...

|                   |          |         |         |         |        |         |
|-------------------|----------|---------|---------|---------|--------|---------|
| depress           | 1.000    |         |         |         | 1.000  | 1.000   |
| .depre1_o         | 0.509    |         |         |         | 0.509  | 0.509   |
| .depre2_o         | 0.569    |         |         |         | 0.569  | 0.569   |
| .depre3_o         | 0.423    |         |         |         | 0.423  | 0.423   |
| .depre4_o         | 0.465    |         |         |         | 0.465  | 0.465   |
| .depre5_o         | 0.632    |         |         |         | 0.632  | 0.632   |
| .depre6_o         | 0.643    |         |         |         | 0.643  | 0.643   |
| Scales y*:        |          |         |         |         |        |         |
|                   | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depre1_o          | 1.000    |         |         |         | 1.000  | 1.000   |
| depre2_o          | 1.000    |         |         |         | 1.000  | 1.000   |
| depre3_o          | 1.000    |         |         |         | 1.000  | 1.000   |
| depre4_o          | 1.000    |         |         |         | 1.000  | 1.000   |
| depre5_o          | 1.000    |         |         |         | 1.000  | 1.000   |
| depre6_o          | 1.000    |         |         |         | 1.000  | 1.000   |
| Group 2 [6]:      |          |         |         |         |        |         |
| Latent Variables: |          |         |         |         |        |         |
|                   | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
| depress =~        |          |         |         |         |        |         |
| depre1_ (.p1.)    | 0.701    | 0.013   | 52.266  | 0.000   | 0.736  | 0.719   |

# Measurement invariance testing - scalar/stroing invariance

...

|    |                |          |         |         |         |        |         |
|----|----------------|----------|---------|---------|---------|--------|---------|
| 40 | depre2_ (.p2.) | 0.656    | 0.014   | 47.410  | 0.000   | 0.689  | 0.653   |
|    | depre3_ (.p3.) | 0.760    | 0.015   | 51.150  | 0.000   | 0.798  | 0.736   |
|    | depre4_ (.p4.) | 0.732    | 0.014   | 52.459  | 0.000   | 0.768  | 0.702   |
|    | depre5_ (.p5.) | 0.607    | 0.016   | 38.229  | 0.000   | 0.637  | 0.598   |
|    | depre6_ (.p6.) | 0.598    | 0.015   | 38.668  | 0.000   | 0.627  | 0.585   |
| 45 | Intercepts:    |          |         |         |         |        |         |
|    |                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|    | depress        | -0.036   | 0.037   | -0.973  | 0.331   | -0.034 | -0.034  |
|    | .depre1_o      | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre2_o      | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre3_o      | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre4_o      | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre5_o      | 0.000    |         |         |         | 0.000  | 0.000   |
|    | .depre6_o      | 0.000    |         |         |         | 0.000  | 0.000   |
| 50 | Thresholds:    |          |         |         |         |        |         |
|    |                | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|    | dpr1_ 1 (.p9.) | -0.585   | 0.027   | -21.689 | 0.000   | -0.585 | -0.572  |
|    | dpr1_ 2 (.10.) | 0.121    | 0.024   | 4.979   | 0.000   | 0.121  | 0.118   |
|    | dpr1_ 3 (.11.) | 1.096    | 0.032   | 34.556  | 0.000   | 1.096  | 1.070   |
|    | dpr1_ 4 (.12.) | 1.795    | 0.046   | 39.323  | 0.000   | 1.795  | 1.754   |
|    | dpr2_ 1 (.13.) | -0.910   | 0.029   | -30.906 | 0.000   | -0.910 | -0.863  |
|    | dpr2_ 2 (.14.) | -0.212   | 0.024   | -8.750  | 0.000   | -0.212 | -0.201  |
| 55 |                |          |         |         |         |        |         |
| 60 |                |          |         |         |         |        |         |

# Measurement invariance testing - scalar/stroing invariance

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|                 |        |       |         |       |        |        |
|-----------------|--------|-------|---------|-------|--------|--------|
| dpr2_  3 (.15.) | 0.746  | 0.027 | 27.431  | 0.000 | 0.746  | 0.708  |
| dpr2_  4 (.16.) | 1.542  | 0.039 | 39.662  | 0.000 | 1.542  | 1.462  |
| dpr3_  1 (.17.) | 0.288  | 0.025 | 11.339  | 0.000 | 0.288  | 0.265  |
| dpr3_  2 (.18.) | 0.685  | 0.028 | 24.794  | 0.000 | 0.685  | 0.631  |
| dpr3_  3 (.19.) | 1.216  | 0.034 | 35.475  | 0.000 | 1.216  | 1.121  |
| dpr3_  4 (.20.) | 1.687  | 0.044 | 38.010  | 0.000 | 1.687  | 1.556  |
| dpr4_  1 (.21.) | -0.125 | 0.025 | -4.968  | 0.000 | -0.125 | -0.114 |
| dpr4_  2 (.22.) | 0.255  | 0.025 | 10.072  | 0.000 | 0.255  | 0.233  |
| dpr4_  3 (.23.) | 0.919  | 0.030 | 30.898  | 0.000 | 0.919  | 0.840  |
| dpr4_  4 (.24.) | 1.496  | 0.039 | 38.146  | 0.000 | 1.496  | 1.368  |
| dpr5_  1 (.25.) | -0.395 | 0.025 | -15.905 | 0.000 | -0.395 | -0.370 |
| dpr5_  2 (.26.) | 0.063  | 0.023 | 2.678   | 0.007 | 0.063  | 0.059  |
| dpr5_  3 (.27.) | 0.682  | 0.027 | 25.599  | 0.000 | 0.682  | 0.639  |
| dpr5_  4 (.28.) | 1.265  | 0.035 | 36.570  | 0.000 | 1.265  | 1.187  |
| dpr6_  1 (.29.) | -0.458 | 0.025 | -18.069 | 0.000 | -0.458 | -0.427 |
| dpr6_  2 (.30.) | 0.076  | 0.024 | 3.238   | 0.001 | 0.076  | 0.071  |
| dpr6_  3 (.31.) | 0.757  | 0.027 | 27.625  | 0.000 | 0.757  | 0.706  |
| dpr6_  4 (.32.) | 1.289  | 0.034 | 37.377  | 0.000 | 1.289  | 1.203  |

## Variances:

|           | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|-----------|----------|---------|---------|---------|--------|---------|
| depress   | 1.102    | 0.073   | 15.039  | 0.000   | 1.000  | 1.000   |
| .depre1_o | 0.506    |         |         |         | 0.506  | 0.483   |
| .depre2_o | 0.637    |         |         |         | 0.637  | 0.573   |

# Measurement invariance testing - scalar/stroing invariance

...

```

.depre3_o      0.540                0.540      0.459
.depre4_o      0.607                0.607      0.507
.depre5_o      0.730                0.730      0.643
.depre6_o      0.755                0.755      0.657

```

Scales y\*:

|          | Estimate | Std.Err | z-value | P(> z ) | Std.lv | Std.all |
|----------|----------|---------|---------|---------|--------|---------|
| depre1_o | 0.977    | 0.025   | 39.050  | 0.000   | 0.977  | 1.000   |
| depre2_o | 0.948    | 0.023   | 41.409  | 0.000   | 0.948  | 1.000   |
| depre3_o | 0.922    | 0.026   | 35.106  | 0.000   | 0.922  | 1.000   |
| depre4_o | 0.914    | 0.025   | 36.803  | 0.000   | 0.914  | 1.000   |
| depre5_o | 0.938    | 0.026   | 35.431  | 0.000   | 0.938  | 1.000   |
| depre6_o | 0.933    | 0.026   | 35.854  | 0.000   | 0.933  | 1.000   |

```

## Conducting a corrected chi-square test
## Comparing the metric and the scalar model
lavTestLRT(fit.metric.WLSMV, fit.scalar.WLSMV,
           method = "satorra.bentler.2010",
           A.method = "delta")

```

# Measurement invariance testing - scalar/strong invariance

...

Scaled Chi Square Difference Test (method = "satorra.bentler.2010")

|                  | Df | AIC | BIC | Chisq  | Chisq diff | Df diff | Pr(>Chisq) |
|------------------|----|-----|-----|--------|------------|---------|------------|
| fit.metric.WLSMV | 23 |     |     | 188.87 |            |         |            |
| fit.scalar.WLSMV | 40 |     |     | 201.38 | 21.469     | 17      | 0.206      |

# References

- Arbuckle, J. L. (1996). Advanced structural equation modeling: Issues and techniques. In G. A. Marcoulides & R. E. Schumacker (Eds.), (p. 243-277). Mahwah, NJ: Lawrence Erlbaum.  
doi:10.4324/9781315827414
- Beauducel, A., & Herzberg, P. Y. (2006). On the performance of maximum likelihood versus means and variance adjusted weighted least squares estimation in CFA. *Structural Equation Modeling*, *13*, 186-203.  
doi:10.1207/s15328007sem1302\_2
- Bollen, K. A., & Barb, K. H. (1981). Pearson's R and coarsely categorized measures. *American Sociological Review*, *46*, 232-239.  
doi:10.2307/2094981

## References ...

- Correll, J., Park, B., Judd, C. M., & Wittenbrink, B. (2002). The police officer's dilemma: Using ethnicity to disambiguate potentially threatening individuals. *Journal of Personality and Social Psychology: Attitudes and Social Cognition*, *83*, 1314-1329.  
doi:10.1037//0022-3514.83.6.1314
- DiStefano, C., & Morgan, G. B. (2014). A comparison of diagonal weighted least squares robust estimation techniques for ordinal data. *Structural Equation Modeling*, *21*, 425-438. doi:10.1080/10705511.2014.915373
- Flora, D. B., & Curran, P. J. (2004a). An empirical evaluation of alternative methods of estimation for confirmatory factor analysis with ordinal data. *Psychological Methods*, *9*, 466-491.  
doi:10.1037/1082-989x.9.4.466

## References ...

- Flora, D. B., & Curran, P. J. (2004b). An empirical evaluation of alternative methods of estimation for confirmatory factor analysis with ordinal data. *Psychological Methods, 9*, 466-491.  
doi:10.1037/1082-989x.9.4.466
- Göllner, R., Roberts, B. W., Damian, R. I., Lüdtke, O., Jonkmann, K., & Trautwein, U. (2017). Whose "strom and stress" is it? Parent and child reports of personality development in the transition to early adolescence. *Journal of Personalily, 85*, 376-387.  
doi:10.1111/jopy.12246
- Lee, S.-Y., & Song, X.-Y. (2003). Bayesian analysis of structural equation models with dichotomous variables. *Statistics in Medicine, 22*, 3073-3088. doi:10.1002/sim.1544



## References ...

- Li, C. -H. (2016). Confirmatory factor analysis with ordinal data: Comparing robust maximum likelihood and diagonally weighted least squares. *Behavior Research Methods*, 48, 936-949. doi:10.3758/s13428-015-0619-7
- Muthén, B., & Kaplan, D. (1985). A comparison of some methodologies for the factor analysis of non-normal likert variables. *British Journal of Mathematical and Statistical Psycholgy*, 38, 171-189. doi:10.1111/j.2044-8317.1985.tb00832.x
- Muthén, B. O. (1993). Testing structural equation models. In K. A. Bollen & S. J. Long (Eds.), (p. 205-243). CA: Newbury Park: Sage.
- O'Brien, R. M. (1985). The relationship between ordinal measures and their underlying values: Why all the disagreement? *Quality and Quantity*, 19, 265-277. doi:10.1007/bf00170998

## References ...

- Song, X.-Y., & Lee, S.-Y. (2002). Bayesian estimation and model selection of multivariate linear model with polytomous variables. *Multivariate Behavioral Research*, *37*, 453-477. doi:10.1207/s15327906mbr3704\_02
- Soto, C. J., & John, O. P. (2017a). The next Big Five Inventory (BFI-2): Developing and assessing a hierarchical model with 15 facets to enhance bandwidth, fidelity, and predictive power. *Journal of Personality and Social Psychology*, *113*, 117-143. doi:10.1037/pspp0000096
- Soto, C. J., & John, O. P. (2017b). Short and extra-short forms of the Big Five Inventory-2: The BFI-2-S and BFI-2-XS. *Journal of Research in Personality*, *68*, 69-81. doi:10.1016/j.jrp.2017.02.004

# Session

```
sessionInfo()
```

```
R version 3.6.0 (2019-04-26)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 19.04

Matrix products: default
BLAS:   /usr/lib/x86_64-linux-gnu/atlas/libblas.so.3.10.3
LAPACK: /usr/lib/x86_64-linux-gnu/atlas/liblapack.so.3.10.3

locale:
 [1] LC_CTYPE=en_US.UTF-8      LC_NUMERIC=C
      LC_TIME=en_US.UTF-8
 [4] LC_COLLATE=en_US.UTF-8   LC_MONETARY=en_US.UTF-8
      LC_MESSAGES=en_US.UTF-8
 [7] LC_PAPER=en_US.UTF-8     LC_NAME=C              LC_ADDRESS=C
[10] LC_TELEPHONE=C          LC_MEASUREMENT=en_US.UTF-8
      LC_IDENTIFICATION=C

attached base packages:
[1] stats      graphics  grDevices  utils      datasets  methods   base

other attached packages:
[1] plyr_1.8.4   lavaan_0.6-3  kutils_1.69
```

# Session ...

```
loaded via a namespace (and not attached):
[1] MASS_7.3-51.4  compiler_3.6.0 tools_3.6.0    foreign_0.8-71
     Rcpp_1.0.1    mnormt_1.5-5
[7] pbivnorm_0.6.0 xtable_1.8-4  zip_2.0.2      openxlsx_4.1.0
     stats4_3.6.0
```